## C. DUMITRESCU V. SELEACU

# SMARANDACHE FUNCTION

(book series)

Vol. 2-3

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### A BRIEF HISTORY OF THE "SMARANDACHE FUNCTION"

by Dr. Constantin Dumitrescu Department of Mathematics University of Craiova, Romania

This function is originated from the exiled Romanian professor Florentin Smarandache. It is defined as follows:

For any non-null integers n, S(n) is the smallest integer such that (S(n))! is divisible by n.

The importance of the notion is that it characterizes a prime number, i.e.:

Let p > 4, then: p is prime if and only if S(p) = p. Another properties:

If (a,b) = 1, then  $S(ab) = \max \{ S(a), S(b) \}$ ; and

For any non-null integers,  $S(ab) \le S(a) + S(b)$ . {All three found and proved by the author in 1979 (see [3], 15, 12-13, 65).}

If n > 1, then S(n) and n have a proper common divisor. {Found and proved by student Prodănescu in 1993: as a lemma needed to solve the conjecture formulated by the author in 1979 that:

the equation S(n) = S(n + 1) has no solutions (see [3], 37, and [30]).} Etc.

Also, an infinity of open/unsolved problems, involving this function, provoked mathematicians around the world to study it and its applications (computational mathematics, simulation, quantum theory, etc.).

Thus, the unsolved question:

Calculate 
$$\lim_{n\to\infty} \left[1 + \sum_{k=2}^{n} \frac{1}{S(k)} - \log S(n)\right], \text{ (see [3], 29)}$$

made by the author in 1979, has been separately proved by J. Thompson from USA in 1992 (see [18], 1), by Nigel Backhouse from United Kingdom in 1993 (see [25]), and by Pål Grønås from Norway in 1993 (see [51]) that this limit is equal to  $\infty$ .

The author wonderred if it's possible to approach the function (see [3], 1979, 25-6), but Ian Parberry expressed that one can immediately find an algorithm that computes S(n) in O(nlogn/loglogn) time (see [38], 1993).

Some unsolved (by now!) other problems stated by the author in 1979 (see [3], 27-30):

- a) To find a general form of the continued fraction expansion of S(n)/n, for all  $n\geq 2$ .
- b) What is the smallest k such that for any integer n at least one of the numbers S(n), S(n+1), ..., S(n+k-1) is a

perfect square?

c) To build the largest arithmetical progression  $a_1$ ,  $a_2$ , ...,  $a_r$  for which their images by the function are also an arithmetical progression.

Etc.

In 1975 Smarandache was a student at the University of Craiova, and he was attracted by the Number Theory. He created and published a lot of proposed problems of mathematics in various scientific journals. He liked to play with the numbers ... Thus, in 1980 his research paper "A Function in the Number Theory", based on a special representation of integers, was published (for the first time) in <a href="#">Analele Universității Timișoara</a>, Seria Științe Matematice, Vol. 18, pp. 79-88,

and was reviewed in <Zentralblatt fur Mathematik>, 471.10004, 1982, by P. Kiss, and in the <Mathematical Reviews>, 83c:10008, 1983, by R. Meyer.

In 1988 he escaped from the Ceauşescu's dictatorship, spent almost two years in a political refugee camp in Turkey (Istambul and Ankara), and finally emigrated to the United States.

Articles, notes, quickies, comments, proposals related to the Smarandache Function were presented to international conferences within the Mathematical Association of America or the American Mathematical Society at the New Mexico State University (Las Cruces), New Mexico Tech. (Socorro), University of Arizona (Tucson), University of San Antonio, University of Victoria (Canada) etc. or published in <Octogon> (Sacele), <Gazeta Matematică> (Bucharest), <The Mathematical Spectrum> (UK), <Elemente der Mathematik> (Switzerland), <The Fibonacci Quarterly> (USA) etc.

In 1992 Dr. J. R. Sutton from United Kingdom designed a BASIC PROCedure to calculate S(n) for all powers of a prime number up to a maximum. (see [26])

Jim Duncan from United Kingdom computed up to S(1499999), the first million taking 50 hours in Lattice C on an Atari 1040ST. (see [17])

Also, John McCarthy from United Kingdom estimated that his machine would take several years to just calculate and store S(n) to disk for the entire range of n it can handle  $(0<n<2^32)$ , and using the compression detailed in ncld9207.c at least 12 Gigabytes of disk space would be needed. It took about 3 hours for his program to work out that 3,303,302 pages (!) would be needed to list the full range of n and S(n). (see [15])

In 1993 Henry Ibstedt from Sweden used a dtk-computer with 486/33 MHz processor in Borland's Turbo Basic and calculated S(n) for n upto  $10^6$  which took 2 hours and 50 minutes! (see [52])

A group of professors (V. Seleacu, C. Dumitrescu, L. Tuţescu, I. Pătrascu, M. Mocanu) and scientific students from the University of Craiova, having a weekly meeting, are doing research on the function and its applicability.

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Prof. Dr. V. Seleacu & Lect. Dr. C. Dumitrescu, Department of Mathematics, University of Craiova, Romania, editors for the next issues;

registered by the Library of Congress (Washington, D. C., USA) under the code: QA .246 .S63;

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The Smarandache Function, together with a sample of The Infinity of Unsolved Problems associated with it, presented by Mike Mudge.<sup>1</sup>

The Smarandache Function, S(n) (originated by Florentin Smarandache — Smarandache Function Journal, vol 1, no 1, December 1990. ISSN 1053-4792) is defined for all non-null integers, n. to be the smallest integer such that (S(n))! is divisible by n.

Note N! denotes the factorial function, N!=1x2x3x...xN: for all positive integer N. In addition 0! = 1 by definition

S(n) is an even function. That is, S(n) = S(-n) since if (S(n))! is divisible by n it is also divisible by -n.

S(p) = p when p is a prime number, since no factorial less than p! has a factor p in this case where p is prime.

The values of S(n) in  $Fig\ 1$  are easily verified. For example, S(14) = 7 because 7 is the smallest number such that 7! is divisible by 14.

Problem (i) Design and implement an algorithm to generate and store/tabulate S(n) as a function of n.

Hint It may be advantageous to consider the STANDARD FORM of n, viz n =  $ep_1^a, p_2^a, \dots, p_r^a$ , where  $e=\pm 1, p_1, p_2, \dots, p_r^a$  denote the distinct prime factors of n and a, a, ......a, are their respective multiplicities.

**Problem (ii)** Investigate those sets of consecutive integers (i.i+1.i+2...i+x) for which S generates a monotonic increasing (or indeed monotonic decreasing) sequence.

Note For (1.2.3,4.5) S generates the monotonic increasing sequence 0.2.3.4.5; here i = 1 & x = 4.

If possible estimate the largest value of x.

Problem (iii) Investigate the existence of integers m,n,p,q & k with n≠m and p≠q for which:

either (A): S(m) + S(m+1) + .... S(m+p) = S(n) + S(m+1) + .... S(n+q) or (B):  $\frac{S(m)^2 + S(m+1)^2 + .... S(m+p)^2}{S(n)^2 + S(n+1)^2 + .... S(n+p)^2} = k$ 

Problem (iv) Find the smallest integer k

for which it is true that <u>for all n less than</u> some given n, at least one of:

S(n), S(n+1)....S(n+k-1) is:

A) a perfect square

B) a divisor of k<sup>a</sup>
C) a factorial of a positive integer.

Conjecture what happens to k as  $n_0$  tends to infinity: i.e. becomes larger

and larger.

Problem (v) Construct prime numbers of the form S(n) S(n+1)...S(n+k): where abcdefg denotes the integer formed by the concatenation of a.b.c.d.e.f & g. For example, trivially S(2) S(3) = 23 which is prime, but no so trivially S(14)S(15)S(16)S(17) = 75617, also prime!

Definition An A-SEQUENCE is an integer sequence a, a, ... with 1≤a, <a, <... such that no a, is the sum of distinct members of the sequence (other than a).

Problem (vi) Investigate the construction of A-SEQUENCES  $a_1, a_2, ...$  such that the associated sequences  $S(a_1), S(a_2), ...$  are also A-SEQUENCES.

Definition The kth order forward finite differences of the Smarandache function are defined thus:

 $D_s(x) = \text{*modulus}(S(x+1) - S(x)),$   $D_s^{(k)} \quad (x) = D(D(...k-\text{times}D_s(x)...))$ **Problem (vii)** Investigate the conjecture that  $D_s^{(k)}(1) = 1$  or 0 for all k greater

than or equal to 2.

c.f. Gilbreath's conjecture on prime numbers, discussed in 'Numbers Count' PCW Dec 1983. \* Here modulus is taken to mean the absolute value of (ABS.), modulus (y) = y if y is positive and modulus (y) = -v if y is negative.

The following selection of Diophantine Equations (i.e. solutions are sought in integer values of x) are taken from the Smarandache Journal and make up:

Problem (viii) If m & n are given integers, solve each of:

a) S(x) = S(x+1), conjectured to have no

solution

b) S(mx+n) = x

c) S(mx+n) = m+nx

d) S(mx+n) = x!

e)  $S(x^m) = x^n$ 

f)  $S(x)^m = S(x^n)$ 

g) S(x) + y = x + S(y), x&y not prime

h) S(x) + S(y) = S(x+y)

i) S(x+v) = S(x)S(v)

i) S(xv) = S(x)S(v)

#### Review, July 1992 The Smarandache Function: a first visit? <sup>2</sup>

This topic is certain to be revisited in the near future, and the lack of space available here will certainly be remedied on that occasion. Suffice it to report that Jim Duncan computed up to S(1499999), the first million taking 50 hours in Lattice C on an Atari 1040ST. In Problem (ii), no evidence for a largest value of x was found, while in Problem (vii) the conjecture was verified for the first 32.000 values of S(n). The very worthy prizewinner is John McCarthy of 17 Mount Street, Mansfield, Norts NG19 7AT, who has extensively investigated the computation of S(n) up to 232; arriving at conclusions such as: 'several years of computing', 'at least 12Gb of disk space' and '3,303,302 pages of output'. John's concluding comment, 'Am I mad?', is clearly answered NO! by examining his specimen pages of output including those relating to 10digit values of n. Listings supplied. Details from John directly upon request.

Republished from <Personal Computer World>, No.112, 420, July 1992 (with the author permission), because some of the following research papers are referring to these open problems.

Republished from <Personal Computer World>, No.117, 412, December 1992 (with the author permission).

# ALGORITHM IN LATTICE C TO GENERATE S(n)

Run time: ca. 50 hrs to generate S(n) for 1 000 000 numbers

by Jim Duncan
9 Ryeground Lane
Formby
Liverpool
L37 7EG ENGLAND

#include <stdio.h> #include <math.h> unsigned long int pst,ast,s,t; main() long int n; FILE \*fp; printf("input n (1 <= n < 2 147 483 647)\n"); scanf("%1d", &n); fp = fopen("PRN:", "w");  $fprintf(fp, "n = %ld S(n) = %ld\n", n, smaran(n));$ fclose(fp): smaran (m) unsigned long int m; unsigned long int mst.p.a.fact: double r: if (m == 1)return(0); /\* STANDARD FORM of m \*/ else { r = mst = m;p = 1;fact = 1; while  $( ++p \le sqrt(r))$ { a = 0;while (mst % p == 0) { mst = mst/p; a++; r = mst;if (a > 0) { pst = p; ast = a;

t = s = 0;

Computer: Atari 1040ST

```
tors3(): /* find smallest factorial (t) with */
                                           /* p^a divsor */
                                  if (t > fact)
                                          fact = t:
                                  3
                         if (mst > fact)
                                 fact = mst:
                         return(fact):
tors1()
            unsigned long int i:
      /* test number is pst^ast */
      /* s is the difference between a factorial number t and ast*(pst-1) */
      /* s forms a pattern which determines the smallest value of t for which */
      /* the test number is a divisor */
            i = 0:
            while (++i < pst*pst && t-s < ast*(pst-1)) {
                    if (i % pst == 0)
                             s = s-pst+2:
                    else
                             5++:
                    t += pst:
   }
   tors2()
    ₹
            unsigned long int i:
            tors1():
            i = 0:
            while (++i < pst*pst && t-s < ast*(pst-1)) {
                    if (i % pst == 0)
                            s = s-3*pst+4;
                    else
                            s = s-2*pst+3:
                    t += pst:
                    tors1():
                    }
   3
   tors3()
           unsigned long int i:
           tors2():
           i = 0;
           while (++i < pst*pst && t-s < ast*(pst-1)) {
                    if (i % pst == 0)
                            s = s-5*pst+6;
                    else
                            s = s-4*pst+5;
                    t += pst;
                    tors2():
   }
```

#### MONOTONIC INCREASING AND DECREASING SEQUENCES OF S(n)

by Jim Duncan

#### Problem (11)

Monotonic increasing and monotonic decreasing sequences of S(n) were investigated for  $x \ge 6$ .

First number	(i)		ոստ	ber of	sequ	iences	S		
in range		× =	6	x =	7	×	= 8	× =	= 9
		inc	dec	inc	dec	inc	dec	inc	dec
1 -	499 999	75	83	7	10		2	0	0
500 000 -	999 999	80	76	14	18	1	3	1	1
1 000 000 - 1	499 999	75	63	8	10	1	2	1	1

There appears to be no evidence for a largest value for x. The sequences for x = 9 are shown in Results Table 1.

The existence of sequences with the same first order finite differences was then considered eq:

i	=	440	S(i)	=	11;	i =	5073	S(i)	=	89
i+1	=	441	S(i+1)	=	14;	i+1 =	5074	S(i+1)	=	59
i+2	=	442	S(i+2)	=	17:	i+2 =	5075	S(i+2)	=	29

Apart from the initial quartet 2,3,4,5 all such sequences with  $i < 1\ 000\ 000$  are triplets. If the first order finite differences are multiples of 6 then the S(n) values appear to be prime numbers. The values are shown in Results Table 2.

#### RESULTS TABLE 1

#### Sequences of S(n)

x = 9

n = 586951 S(n) = 586951 n = 586952 S(n) = 73369 n = 586953 S(n) = 21739 n = 586954 S(n) = 9467 n = 586955 S(n) = 1319 n = 586956 S(n) = 1193 n = 586957 S(n) = 1181 n = 586958 S(n) = 1091 n = 586959 S(n) = 677 n = 586960 S(n) = 29

x = 9

n = 721970 S(n) = 73 n = 721971 S(n) = 827 n = 721972 S(n) = 907 n = 721973 S(n) = 6067 n = 721974 S(n) = 10939 n = 721975 S(n) = 28879 n = 721976 S(n) = 90247 n = 721977 S(n) = 240659 n = 721978 S(n) = 360989 n = 721979 S(n) = 721979

x = 9

n = 1091150 S(n) = 157 n = 1091151 S(n) = 709 n = 1091152 S(n) = 1451 n = 1091153 S(n) = 1607 n = 1091154 S(n) = 6271 n = 1091155 S(n) = 16787 n = 1091156 S(n) = 24799 n = 1091157 S(n) = 363719 n = 1091158 S(n) = 545579 n = 1091159 S(n) = 1091159

x = 9

n = 1473257 S(n) = 1473257 n = 1473258 S(n) = 8467 n = 1473259 S(n) = 6323 n = 1473260 S(n) = 3877 n = 1473261 S(n) = 3533 n = 1473262 S(n) = 2239 n = 1473263 S(n) = 1999 n = 1473264 S(n) = 787 n = 1473265 S(n) = 557 n = 1473266 S(n) = 463

```
same difference = 1 n = 4 S(n-2) = 2 S(n-1) = 3 S(n) = 4
 same difference = 1 n = 5 S(n-2) = 3 S(n-1) = 4 S(n) = 5
  same difference = 11 n = 18 S(n-2) = 6 S(n+1) = 17 S(n) = 6
 same difference = 3 \cdot n = 442 \cdot S(n-2) = 11 \cdot S(n-1) = 14 \cdot S(n) = 17
 same difference = 30 n = 5075 S(n-2) = 89 S(n-1) = 59 S(n) = 29
 same difference = 60 \cdot n = 6409 \cdot S(n-2) = 149 \cdot S(n-1) = 89 \cdot S(n) = 29
 same difference = 48 n = 6479 S(n-2) = 127 S(n-1) = 79 S(n) = 31
 same difference = 36 n = 8177 S(n-2) = 109 S(n-1) = 73 S(n) = 37 same difference = 84 n = 13717 S(n-2) = 211 S(n-1) = 127 S(n) = 43
 same difference = 168 n = 20468 S(n-2) = 379 S(n-1) = 211 S(n) = 43
 same difference = 210 n = 22591 S(n-2) = 461 S(n-1) = 251 S(n) = 41
 same difference = 120 n = 35145 S(n-2) = 311 S(n-1) = 191 S(n) = 71
 same difference = 180 n = 59719 S(n-2) = 449 S(n-1) = 269 S(n) = 89
 same difference = 150 n = 67771 S(n-2) = 401 S(n-1) = 251 S(n) = 101
 same difference = 264 \cdot n = 73425 \cdot S(n-2) = 617 \cdot S(n-1) = 353 \cdot S(n) = 89
 same difference = 840 n = 74005 S(n-2) = 1721 S(n-1) = 881 S(n) = 41
 same difference = 24 n = 82297 \text{ S}(n-2) = 151 \text{ S}(n-1) = 127 \text{ S}(n) = 103
 same difference = 60 \cdot n = 104669 \cdot S(n-2) = 251 \cdot S(n-1) = 191 \cdot S(n) = 131
 same difference = 330 \text{ n} = 111507 \text{ S(n-2)} = 769 \text{ S(n-1)} = 439 \text{ S(n)} = 109
 same difference = 36 \cdot n = 114427 \cdot S(n-2) = 199 \cdot S(n-1) = 163 \cdot S(n) = 127
 same difference = 252 n = 120523 S(n-2) = 631 S(n-1) = 379 S(n) = 127
 same difference = 120 n = 129928 S(n-2) = 389 S(n-1) = 269 S(n) = 149
 same difference = 952 \text{ n} = 146004 \text{ S(n-2)} = 1973 \text{ S(n-1)} = 1021 \text{ S(n)} = 69
 same difference = 600 \text{ n} = 153520 \text{ S(n-2)} = 1301 \text{ S(n-1)} = 701 \text{ S(n)} = 101
 same difference = 12 n = 180482 \text{ S}(n-2) = 47 \text{ S}(n-1) = 59 \text{ S}(n) = 71
 same difference = 660 \, \text{n} = 181485 \, \text{S(n-2)} = 1429 \, \text{S(n-1)} = 769 \, \text{S(n)} = 109
 same difference = 60 \text{ n} = 189954 \text{ S(n-2)} = 53 \text{ S(n-1)} = 113 \text{ S(n)} = 173
 same difference = 90 n = 192067 S(n-2) = 359 S(n-1) = 269 S(n) = 179
 same difference = 324 \text{ n} = 198697 \text{ S(n-2)} = 811 \text{ S(n-1)} = 487 \text{ S(n)} = 163
same difference = 336 n = 209752 \text{ S}(n-2) = 839 \text{ S}(n-1) = 503 \text{ S}(n) = 167 \text{ same difference} = 228 n = <math>227099 \text{ S}(n-2) = 647 \text{ S}(n-1) = 419 \text{ S}(n) = 191 \text{ same difference} = 150 n = <math>231039 \text{ S}(n-2) = 499 \text{ S}(n-1) = 349 \text{ S}(n) = 199 \text{ same difference}
same difference = 264 \text{ n} = 253725 \text{ S(n-2)} = 727 \text{ S(n-1)} = 463 \text{ S(n)} = 199
same difference = 210 n = 266915 S(n-2) = 631 S(n-1) = 421 S(n) = 211
same difference = 648 n = 297638 S(n-2) = 1459 S(n-1) = 811 S(n) = 163
same difference = 2808 n = 306128 S(n-2) = 5669 S(n-1) = 2861 S(n) = 53
same difference = 1320 \text{ n} = 324384 \text{ S(n-2)} = 2749 \text{ S(n-1)} = 1429 \text{ S(n)} = 109
same difference = 18 n = 326163 \text{ S}(n-2) = 199 \text{ S}(n-1) = 181 \text{ S}(n) = 163
same difference = 240 n = 342965 S(n-2) = 719 S(n-1) = 479 S(n) = 239
same difference = 36 	 n = 346390 	 S(n-2) = 139 	 S(n-1) = 103 	 S(n) = 67
same difference = 300 \text{ n} = 386906 \text{ S(n-2)} = 47 \text{ S(n-1)} = 347 \text{ S(n)} = 647
same difference = 840 n = 409422 \text{ S}(n-2) = 1861 \text{ S}(n-1) = 1021 \text{ S}(n) = 181

same difference = 270 n = 440375 \text{ S}(n-2) = 811 \text{ S}(n-1) = 541 \text{ S}(n) = 271
same difference = 936 n = 443450 S(n-2) = 2053 S(n-1) = 1117 S(n) = 181
same difference = 120 n = 443850 S(n-2) = 509 S(n-1) = 389 S(n) = 269
same difference = 792 n = 443969 S(n-2) = 1783 S(n-1) = 991 S(n) = 199
same difference = 450 n = 450043 S(n-2) = 1151 S(n-1) = 701 S(n) = 251
same difference = 306 n = 451215 S(n-2) = 883 S(n-1) = 577 S(n) = 271
same difference = 210 n = 460559 S(n-2) = 701 S(n-1) = 491 S(n) = 281
same difference = 240 n = 464212 \text{ S(n-2)} = 761 \text{ S(n-1)} = 521 \text{ S(n)} = 281
same difference = 360 \text{ n} = 470727 \text{ S(n-2)} = 991 \text{ S(n-1)} = 631 \text{ S(n)} = 271
same difference = 624 - n = 473922 S(n-2) = 1481 S(n-1) = 857 S(n) = 233
same difference = 90 n = 481779 S(n-2) = 449 S(n-1) = 359 S(n) = 269
same difference = 126 n = 511688 S(n-2) = 131 S(n-1) = 257 S(n) = 383
same difference = 672 \cdot n = 512894 \cdot S(n-2) = 1583 \cdot S(n-1) = 911 \cdot S(n) = 239
same difference = 480 n = 521946 S(n-2) = 1231 S(n-1) = 751 S(n) = 271
same difference = 714 n = 531775 S(n-2) = 1667 S(n-1) = 953 S(n) = 239
same difference = 726 \cdot n = 543455 \cdot S(n-2) = 1693 \cdot S(n+1) = 967 \cdot S(n) = 241
```

```
same difference = 306 \text{ n} = 565187 \text{ S(n-2)} = 919 \text{ S(n-1)} = 613 \text{ S(n)} = 307
same difference = 552 \text{ n} = 574498 \text{ S(n-2)} = 1381 \text{ S(n-1)} = 829 \text{ S(n)} = 277
same difference = 1176 n = 586272 \text{ S}(n-2) = 2549 \text{ S}(n-1) = 1373 \text{ S}(n) = 197
same difference = 3444 n = 592537 S(n-2) = 6971 S(n-1) = 3527 S(n) = 83
same difference = 370 \text{ m} = 609871 \text{ S(n-2)} = 1091 \text{ S(n-1)} = 701 \text{ S(n)} = 311
same difference = 840 n = 629508 S(n-2) = 1931 S(n-1) = 1091 S(n) = 251
same difference = 336 n = 681077 S(n-2) = 1009 S(n-1) = 673 S(n) = 337
same difference = 612 \cdot n = 705793 \cdot S(n-2) = 1531 \cdot S(n-1) = 919 \cdot S(n) = 307
same difference = 78 n = 724319 S(n-2) = 467 S(n-1) = 389 S(n) = 311
same difference = 264 n = 726827 S(n-2) = 881 S(n-1) = 617 S(n) = 353
same difference = 498 n = 731179 S(n-2) = 1327 S(n-1) = 829 S(n) = 331
same difference = 240 n = 751746 S(n-2) = 839 S(n-1) = 599 S(n) = 359
same difference = 1356 n = 778837 S(n-2) = 2939 S(n-1) = 1583 S(n) = 227
same difference = 1020 \text{ n} = 792675 \text{ S(n-2)} = 2311 \text{ S(n-1)} = 1291 \text{ S(n)} = 271
same difference = 2214 \text{ n} = 803427 \text{ S(n-2)} = 4591 \text{ S(n-1)} = 2377 \text{ S(n)} = 163
same difference = 1590 n = 810451 S(n-2) = 3391 S(n-1) = 1801 S(n) = 211
same difference = 252 n = 837969 S(n-2) = 883 S(n-1) = 631 S(n) = 379
same difference = 552 \text{ n} = 898783 \text{ S(n-2)} = 1471 \text{ S(n-1)} = 919 \text{ S(n)} = 367
same difference = 2850 m = 930311 \text{ S}(n-2) = 5851 \text{ S}(n-1) = 3001 \text{ S}(n) = 151
same difference = 540 n = 941057 S(n-2) = 1459 S(n-1) = 919 S(n) = 379
same difference = 240 n = 943553 S(n-2) = 881 S(n-1) = 641 S(n) = 401
same difference = 120 n = 975546 S(n-2) = 619 S(n-1) = 499 S(n) = 379
same difference = 1122 n = 997443 S(n-2) = 2551 S(n-1) = 1429 S(n) = 307
same difference = 264 \text{ n} = 1026550 \text{ S(n-2)} = 947 \text{ S(n-1)} = 683 \text{ S(n)} = 419
same difference = 684 \text{ n} = 1028985 \text{ S(n-2)} = 1747 \text{ S(n-1)} = 1063 \text{ S(n)} = 379
same difference = 744 n = 1042162 S(n-2) = 1861 S(n-1) = 1117 S(n) = 373 same difference = 510 n = 1053175 S(n-2) = 1429 S(n-1) = 919 S(n) = 409
```

# ON THE CONJECTURE D<sub>(k)</sub> (1)=1 or 0 for k>=2

by Jim Duncan

#### Problem(vii)

For the first 32 000 S(n)'s the conjecture that  $D_S$  (\*)(1) = 1 or 0 for  $k \geq 2$  is true. The ratio of the number of ones to the number of zeros appears to be approximately 1 for large values of k. The results are shown in Results Table 3.

The true differences S(x-1) - S(x) were calculated and the  $k^{\pm h}$  order differences  $D_s^{++(k-)}(1)$  were found to increase rapidly with increasing k. For large values of k ( > 100) the ratio  $D_s^{++(k-)}(1)/D_s^{++(k-1)}(1)$  is approximately equal to -2. Some values are shown in Results Table 4.

RESULTS TABLE 3

k  $D_s^{(k)}(1)$  Ratio: total 1's total 0's

D1 = 2D1000 = 0 st1/st0 = 1.112051 D2000 = 0 st1/st0 = 1.056584 D3000 = 0 st1/st0 = 1.075433 D4000 = 0 st1/st0 = 1.015625 D5000 = 0 st1/st0 = 1.010861 D6000 = 1 sti/st0 = 0.991039D7000 = 0 st1/st0 = 0.990048 D8000 = 0 st1/st0 = 0.977014D9000 = 0 st1/st0 = 0.987412D10000 = 0 st1/st0 = 0.998201D11000 = 1 st1/st0 = 1.011154D12000 = 1 st1/st0 = 1.010556D13000 = 1 st1/st0 = 1.015036 D14000 = 0 st1/st0 = 1.018601D15000 = 1 st1/st0 = 1.012748D16000 = 0 st1/st0 = 1.004134D17000 = 0 st1/st0 = 1.00530B D18000 = 0 st1/st0 = 1.004789D19000 = 1 sti/st0 = 1.003903D20000 = 1 st1/st0 = 1.004711D21000 = 0 sti/st0 = 1.008129D22000 = 0 st1/st0 = 1.004830 D23000 = 0 st1/st0 = 1.004620D24000 = 0 st1/st0 = 1.003590 D25000 = 1 st1/st0 = 1.004571D26000 = 1 st1/st0 = 1.001001 D27000 = 0 st1/st0 = 1.001260D28000 = 1 st1/st0 = 1.004080D29000 = 0 st1/st0 = 1.006018D30000 = 1 st1/st0 = 1.005415D31000 = 0 st1/st0 = 1.006408D32000 = 1 sti/st0 = 1.004699

k  $D_s^{*(k)}(1)$   $D_s^{*(k)}(1)$   $D_s^{*(k-1)}(1)$ 

0951 = 2.244421E + 298ratio = -2.002974D952 = -4.496445E+288 ratio = -2.0033870953 = 9.009914E + 288ratio = -2.0037870954 = -1.805740E + 289ratio = -2.004170p955 = 3.619671E + 289ratio = -2.004535D956 = -7.257009F + 289ratio = -2.004881D957 = 1.455178E + 290ratio = -2.005204D958 = -2.918366E + 290ratio = -2.0055040959 = 5.853595E + 290ratio = -2.0057780960 = -1.174247E + 291ratio = -2.0060260961 = 2.355827E + 291ratio = -2.0062460962 = -4.726819E + 291ratio = -2.0064370963 = 9.484823E + 291ratio = -2.006598D964 = -1.903346E + 292ratio = -2.006728D965 = 3.819685E + 292ratio = -2.006827 $0^{9}55 = -7.665702E + 292$ ratio = -2.0068940967 = 1.538452E + 293ratio = -2.006929D968 = -3.087569E + 293ratio = -2.006932D969 = 6.196454E + 293ratio = -2.006904D970 = -1.243531E+294ratio = -2.0068430971 = 2.495458E + 294ratio = -2.006751D972 = -5.007457E + 294ratio = -2.006629D973 = 1.004734E+295ratio = -2.006476D974 = -2.015791E + 295ratio = -2.006293D975 = 4.043841E+295ratio = -2.006081D976 = -8.111306E + 295ratio = -2.005842D977 = 1.626784E + 296ratio = -2.005576D978 = -3.262162E + 296ratio = -2.005283D979 = 6.540525E + 296ratio = -2.004966D980 = -1.311130E + 297ratio = -2.004625D981 = 2.627848E + 297ratio = -2.004262D982 = -5.265885E+297 ratio = -2.003877D983 = 1.055006E + 298ratio = -2.003473D984 = -2.113228E + 298ratio = -2.003049D985 = 4.231969E + 298ratio = -2.002608D986 = -8.473041E + 298ratio = -2.002151D987 = 1.696031E + 299ratio = -2.001679D988 = -3.394086E + 299ratio = -2.001193D989 = 6.790531E+299ratio = -2.000695D990 = -1.358233E+300ratio = -2.000186D991 = 2.716013E+300 ratio = -1.999667D992 = -5.429688E+300 ratio = -1.999139D993 = 1.085180E+301 ratio = -1.998604D994 = -2.168257E + 301ratio = -1.998063D995 = 4.331129E+301ratio = -1.997516D996 = -8.649119E + 301ratio = -1.996966D997 = 1.726721E+302ratio = -1.996413D998 = -3.446291E + 302ratio = -1.995858D999 = 6.876396E + 302ratio = -1.995303D1000 = -1.371668E + 303ratio = -1.994748

#### A Simple Algorithm to Calculate S(n)

by John C. McCarthy

#### Introduction

This short paper first outlines an "obvious" algorithm for calculating S(n) (the smallest integer m such that m! is divisible by n). Doubtless, there exist more subtle and efficient algorithms. I hope some readers will devise these and enlighten me concerning them through this journal.

This is followed by a small scale investigation of the efficiency of the algorithm.

Then there is a short discussion of a simple way of reducing the space required for storage of all S(n) for ranges of n. The storage space required for S(n) for all n which my routines can handle is considered.

Heavily commented listings of an implementation of the algorithm in "C", sample output and timing data are included to help illustrate the algorithm.

#### The Algorithm

The algorithm is described in detail at the start of the header file "S(n).H". Together with "S(n).C", this forms all the code necessary to implement the algorithm. Note that, for the S(n) function to work correctly, the function make\_primes() must first be called from the main program.

The code for printing S(n) and timing the routines has been omitted. These activities are both implementation specific and easily done. They are therefore left as an exercise for the interested reader.

The algorithm hinges on finding the prime factors of n. Improvements on how this is done will most benefit its efficiency.

To be practical, the given implementation of the algorithm only works for  $0< n<2^{3/2}$ . However, the algorithm is generally applicable to any non-null integer.

Tables of S(n), constructed using the routines of "S(n).C", for the largest 2000 permitted n are included. My paging routines are rather elaborate. Using them (without printing!), it took 2.4 hours to discover that 3,745,708 pages, as tightly packed as those shown, would be required to print S(n) for all  $0 < n < 2^{32}$ .

#### Efficiency of the Algorithm

In a letter to R. Muller (about computing the Smarandache Function, July 19, 1993), Ian Parberry (editor of <SIGACT News>,

For the smallest 4800 numbers, see Ibstedt's table (pp. 43-50) of this current journal.

Denton, Texas) expressed that one can immediately find an algorithm that computes S(n) in  $O(n\log n/\log\log n)$  time ('A Brief History of the "Smarandache Function"' by Dr. Constantin Dumitrescu, Department of Mathematics, University of Craiova, Romania). Disappointingly, a little analysis of the accompanying timing data on my TI85 advanced scientific calculator reveals that my algorithm is somewhat worse than this.

Trying to fit the version 2 timing data to various O(f(n)), I obtained the following results (x=3355443200 and 10(O(x+99)-O(x-100)) is calculated for comparison with the last entry of the version 1 timing data):

O(f(n))	Correlation Coefficient	0(2 <sup>3</sup> 2-1) (years)	10(O(x+99)-O(x-100) (milliseconds)
O(n)	0.9928879	0.6092	8909
O(nlogn/loglogn)	0.9944006	0.7906	11827
O(n/n)	0.9997756	24.2	469178

O(n/n) fits the version 2 timing data best, although the time it predicts for the last entry of the version 1 timing data is almost 3 times too large. Hence, I assume the time complexity of my algorithm is a little better than O(n/n).

As a rough upper limit on the time my program (on my 20MHz 368DX PC) would take to calculate S(n) for all  $0 < n < 2^{32}$ , let us assume that every value of n requires as much time as each n in the range of the last entry of the version 1 timing data (= 159111/199/10 = 79.9553 ms). In this "worst case", it would take 10.882 years. O(n/n) time complexity predicts more than twice this value, which is a measure of how pessimistic it is.

I would welcome a more rigorous analysis of the time complexity of my algorithm as I presently lack the necessary expertise.

#### Simple Compression of Stored S(n)

Without compression, each S(n) would be stored as a 32-bit (= 4 bytes) value. Hence  $2^{3.4}$  bytes (= 16 Gigabytes) would be required to store S(n) for all  $0 < n < 2^{3.2}$ .

This requirement can be reduced considerably if we use the high bit of each each byte of each value to indicate if it is the last byte of the value. If the bit is set it means that further byte(s) are required and if it is reset it means that the byte is the last byte of the current value. This means that only 7 bits of each byte are used to form the numerical part of the value. Assuming that, as with Intel format, the values are stored low-'byte' (actually 7 bits) first, here are some examples:

- i) 127 requires seven bits and so just one byte (with high bit reset to indicate no further bytes).
- ii) 16,000 requires 14 bits. So it is stored as two bytes. The

first is 0 (16,000 mod 128) + 128 (to set the high bit indicating there is more to come). The second is 125 (16,000 div 128) (with high bit reset to indicate no further bytes). This reads simply as 0 (with more to follow) + 128\*125 (no more to follow).

iii) A number stored as the three bytes 57+128, 93+128 and 125+0
would similarly represent:
57 + 93\*128 + 125\*128\*128 = 2,059,961.

The largest numbers that can be represented by a given number of bytes is thus as follows:

- 1 byte can code up to  $2^7-1 = 127$ .
- 2 bytes can code up to  $2^{14}-1 = 16,383$ .
- 3 bytes can code up to  $2^{21}-1 = 2,097,151$ .
- 4 bytes can code up to  $2^{28}-1 = 268.435.455$ .
- 5 bytes can code up to  $2^{35}-1 = 34,359,738,355$  (or 8 times the largest unsigned long).

For small values of n, the savings are considerable (400%). However, even large n often have small S(n).

Using this technique to compress all S(n) calculated for some ranges of n (each range was also stored), I obtained the following results:

range of n	compression	time taken (seconds)	size	size after pkzip
1	without	4.5	40,008	19,836
-10,000	with	4.7	15,749	15,267
2,147,478,648	without	827.3	40,008	33,729
-2,147,488,647	with	842.4	33,541	30,836
4,294,957,296	without	1,066.2	40,008	34,320
-4,294,967,295	with	1,085.1	34,330	31,634

The results indicate that this compression is a little better than pkzip's (a commercial file compression utility). Application of pkzip to a pre-compressed file also gives a slight improvement.

Assuming that the savings shown for the middle range of 10,000 n are the average of all ranges of 10,000 n, using my compression together with that of pkzip would permit storage of S(n) for all  $0 < n < 2^{3/2}$  in about  $3.0836 * 2^{3/2} = 12.3344$  Gigabytes. So look out for sets of 19 CD-ROMs with all your favourite numbers on them!

21st November 1993

```
/* (c).1993.11.13.John.C.McCarthy
   "S(n).h"
```

Example Implementation of A Simple Algorithm to Calculate S(n), The Smarandache Function:

Because there are more people familiar with C than with C++, this module has been written entirely in C (apart from "//" style comments). module was compiled using Borland C++ version 3.1.

For efficiency, m is constrained to the limits of an unsigned long. Hence,  $0 \le n \le 2^32 - 1 (= 4,294,967,295)$ . ("^" represents exponentiation). Although catering for n of vast magnitude is possible, it imposes heavy storage and processing overheads. The range of an unsigned long therefore seems a reasonable compromise.

The algorithm depends on the most elementary properties of S(n):

- 1) Calculate the STANDARD FORM (SF) of n: In SF:  $n = +/-(p1^a1)*(p2^a2)*...*(pr^ar)$  where p1, p2,...pr denote the distinct prime factors of n and al, a2,...ar are their respective multiplicities.
- 2)  $S(n) = max[S(p1^a1),...,S(pr^ar)].$
- 3) S(p^a), where p is prime, is given by:

  - 3.1)  $a \le p \implies S(p^a) = p^a$ . 3.2)  $a > p \implies S(p^a) = x \le p^a$ . In this case, fortunately rare, x is the smallest integer such that p appears as a factor in the list of all integers > 1 and <= x at least a times. Let the no. of times p appears as a factor in the list of all integers > 1 and  $\langle = y \text{ be } f(y, p) \rangle$ . Then:  $f(y, p) = \Sigma[int(y/(p^i))]$  for i>0 while  $y>=(p^i)$ . Hence, x is the smallest integer such that f(x, p) = a. Note that between succesive integer multiples of p there are no integers which have p as a factor. The trick here is to look for the largest multiple of p (call it c), such that f(p\*c, p) = a

(so that x = p\*c, if f(p\*c, p) = a, else x = p\*(c+1)):

- 3.2.1) c = a-2 (largest possibilty for c since f(p\*(a-1), p) >= awhen a>p (Note: f(p\*(a-1), p)=a is not sought for slight performance gain)).
- 3.2.2) z = f(p\*c, p).
- 3.2.3) While(z>a):
  - 3.2.3.1) d = no. of times p appears as a factor of p\*c = (no. of times p appears as a factor of c) + 1. 3.2.3.2) c = c-1 (next largest possibility for c).
  - 3.2.3.3) z = z-d (= f(p\*c, p)).
- 3.2.4) If (z < a), x = p\*(c+1).
- x = p \* c. 3.2.5) Else

To calculate the prime factors of all 32-bit n requires use only of primes < (2^16) (i.e. all primes expressible as an unsigned short integer). This is because any factor of n remaining after division of n by all its prime factors  $< (2^16)$  is simply a prime. Since there are only 6542 16-bit primes, the program first creates a list of these (which only takes about 4 seconds on my 20 MHz 386DX PC) so that they never have to be recalculated, thus saving much time.

\*/

```
#define PRIMES16 6542 // The number of 16-bit primes
#define MAX SFK 9 /* max. distinct primes in the SF of n. The smallest
    number with more than 9 distinct primes is the product of the 10 smallest
    primes (= 6,469,693,230), which is substantially more than the largest
    integer expressible as an unsigned long. Hence, 9 distinct primes are
    more than ample.
typedef unsigned long u_long;
typedef unsigned int u_int;
typedef enum {false, true} boolean:
struct SF_struct {
      sfk;
                           // no. of distinct primes
  int
                           // the distinct primes
  u_long sfp[MAX_SFK];
  int
                          // respective multiplicities
        sfa[MAX SFK];
extern u int prime[PRIMES16+1]; // list of all 16-bit primes
                                 // plus terminating zero.
void make primes(void); // construct list of all 16-bit primes (prime[]).
                         // Must be called before calls to getSF() or S().
void getSF(u_long n, struct SF_struct *SF); // calc. SF of n and store in SF
u_long S(u_long n); // calc. S(n)
u_long Spa(u_long p, int a); // calc. S(p^a) where p is prime
int f(int x, int p); /* the number of times the prime p appears as a factor
    in the integers from 1 to x inclusive. This function is only called from
    Spa(p, a) when a>p with x=p*(a-2) (refer to item (3) of algorithm outline
    above). Max value of (a) occurs when p is a minimum, n is a maximum and
    (p^a)=n. So, (2^max(a))=max(n)=(2^32)-1. Hence max(a)<32. So, x<60
    when (a) is at its max. Max value of p (and x) occurs when a=p+1 and
    (p^a)=\max(n). So, \max(p)^{(\max(p)+1)}=(2^32)-1. The upshot is that
    \max(p)=9 when a=10. Hence, \max(x)=72. This explains why it is safe for
    x, p and the return value of f(x,p) to be passed as ints.
*/
```

```
/* (c).1993.11.13.John.C.McCarthy
    "S(n).c"
    Example Implementation of A Simple Algorithm to Calculate S(n),
    The Smarandache Function:
   This is the code for the module. Refer to "S(n).h" for details.
* /
#include "S(n).h"
u int prime[PRIMES16+1]; // allocate storage for list of all 16-bit primes
                          // plus terminating zero.
void make_primes(void)
  u int *pp;
              // ptr to last prime so far of prime list
  u_int *tp; // ptr to current test prime
              // number being tested for primality
  u int p;
  pp=prime:
             // point to start of prime list
             // set first prime to 2
             // set second prime to 3
  *++pp=3;
             // next possible prime. N.B. p is kept odd so that trial
  p=5;
             // division by 2 is unnecessary.
  while(true) { // infinite loop!:
                   // point to first odd test prime
    tp=prime+1:
    // whilst test prime <= /p:
    while(((long) *tp)*(*tp)<=p) {
      if(!(p%*tp)) { // If current test prime divides (is factor of) p:
        p+=2:
                         // try next odd number
                         // done when p overflows:
        if(p<*pp) {
          *++pp=0;
                            // terminate list
          return:
                        _// point to first odd test prime
        tp=prime+1:
      3
      else ++tp;
                      // Else point to next test prime
    // no prime <= √p divides p so p must be prime:
    *++pp=p;
                // so store it next in the list
    p+=2:
                 // try next odd number
    if(p<*pp) {
                 // done when p overflows:
                    // terminate list
      *++pp=0;
     return;
    }
 }
}
```

```
void getSF(u_long n, struct SF_struct *SF)
  u_int *pp;
              // ptr to current prime
  u_long r;
              // 'residue' of m remaining for factoring
  SF->sfk=0; // no. of distinct prime factors discovered
  r=n:
  pp=prime;
              // point to start of prime list
  // whilst current prime <= \r and prime list not exhausted:
  while(((long) *pp)*(*pp)<=r && *pp) {
    if(!(r%*pp)) {
                              // if current prime is a factor of r:
                                 // store current prime as next prime of SF
      SF->sfp[SF->sfk]=*pp;
                                 // set its multiplicity to 1
// 'divide out' current prime
      SF->sfa[SF->sfk]=1:
      r/=*pp;
      while(!(r%*pp)) {
                                 // while current prime factors r:
        SF->sfa[SF->sfk]++;
                                    // increment multiplicity
                                    // 'divide out' current prime
        r/=*pp;
      3
      SF->sfk++;
                                 // increment count of distinct prime factors
    3
    ++pp;
                             // next prime
  if(r>1) {
                          // If n contains prime > 2^16:
    SF->sfp[SF->sfk]=r;
                            // store it as last prime of SF
    SF->sfa[SF->sfk]=1;
                            // set its multiplicity to 1
                            // increment count of distinct prime factors
    SF->sfk++:
  }
}
```

```
u long S(u long n)
                         // to store SF of n
  struct SF struct SF:
                         // index of current term of SF of n
// current guess at S(n)
  int sfi:
  u_long Sn;
                         // S(current term of SF of n) where it might exceed
  u long x;
                         // current value of Sn.
  if(n==1) return 0:
                         // special case
  getSF(n, &SF):
                         // calc. and store SF of n
  // First guess at S(n) is S(p^a), where p is the largest prime in the SF
  // of n and a is its multiplicity. This pre-empts the calculation of S(p^a)
  // for the remaining terms where, as is likely, p*a for these terms is <=
  // this initial guess (since S(p^a) <= p*a always):
  sfi=SF.sfk-1;
  Sn=Spa(SF.sfp[sfi],SF.sfa[sfi]);
  while(sfi>0) { // while more term(s):
    sfi--:
                      // next term
    if(SF.sfp[sfi]*SF.sfa[sfi]>Sn) { // if this term may have larger S(p^a):
      x=Spa(SF.sfp[sfi],SF.sfa[sfi]); // calc. it
                                          // if new max., update Sn with it
      if(x>Sn) Sn=x;
    },
  1
  return Sn; // That's all folks!
}
u_long Spa(u_long p, int a)
  // Refer to item 3) of the algorithm description in S(n).h.
  int c: // largest multiple of p such that f(p*c, p) \le a (eventually!)
  int z; // f(p*c, p)
  int m:
         // used to calc. no. of times p appears as factor of c
  if(a<=p) return p*a;
  c=a-2:
  z=f(p*c, p);
  while(z>a) {
    // d in items 3.2.3.1) and 3.2.3.3) of algorithm description is implicit
    // here:
    2--;
   m=c--;
   while(!(m%p)) { // while p divides m:
      z--;
     m/=p;
                        // 'divide out' factor of p from m
    }
  if(z<a) return p*(c+1);
 else return p*c;
}
```

SMARANDAC	HE FUNCTION	S(h), for	n=429496529	6 to n=4294	967295					Page 1 of 2
	\S of a pi	• 1	. 2	3					, ,	
429496525 429496530					14316551					
429496531	16 107374132	9 4583741	102261079	27356467	5174657 1602599	86569 4919777	2147482681	7 429496531: 2296772:		
429496532 429496533	26 214748266 36 2151		7255009 5520521		57427 12632251	4294965331		7557	7 85889	858993067
429496534	16 391	9 4294965347	6911	90407	83641	40139863 1431655117	1228537	2545915		4621 1493
429496535 429496536		9 158597 9 30971	4975419	108907 1431555123	Z339 195137	4294965361	2147482681	23719	118423	38629
429496537	66 41 76 552 86 214748269		154573	279857	1199711	204522161	39107	4294965383	6628033	1307 858993077
429496539	6 35791378	3 4040419			7535027 1852257		268435337 70867	5749619 26349481	2147482697 511549	86357
429496540 429496541		9 2347	154807	529393	5167	14461163	672349	4294965415	34301	24683
429496542			22138997 12109		23860919 321239		17747791 57 <b>728</b> 03	Z045ZZ163 746561		
429496543 429496544	6598	3 1530091	79536397	2473	13421767	1551089	308857	2617	28871	858993089
429496545			35097 357067		28633103	11731 4294965461	121313 415937	13997	2465537 536870683	
429496546	6 1627503	7 14364433	7615187	1822217	40699	88873	169681	4001	5549051	5079
429496547 429496548		7 1154041 3 4294965487	2147482739	1935541 973253	15233 18673763		718943 7253		1073741371	
429496549	6 5095	1 14387	715827583	390451409	1227133	835759	16909313			
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429496552	6 214748276	3 252645031	57193	4294965529	384509	103391	32789		1073741381 12132671	
429496553 429496554			88919 1073741387	3296213	2468371 2321603	6529	2306641	11831861	64319	106747
429496555	6 494811	7 28355287	1038937	12569	28057	622549 2293	89478449 7561	179623 77933		
429496558		1 1431655189 9 1618909	67108837	397057 1431855193	20452217	19709	51829	20507	298801	1831
429498558	6 1970167	7 139	2843	2549	11302541 429496559	4294965581 9739151	10374613 8801159	12781 72796027	2949839 2970239	
429496559		218941 3 118361	961783 536878781	226050821	198841	4294965601	2147482801	33294307	40459	5335361
429496561	<b>6</b> 51523:	1 4294965617	2957	923053 89611	9283 5147	35527 7495577		4294965613		Z1859 3061
429496562		3 1828423 7 682933	46684409 2147482819	2459 1431655213	251689	9137 4294965641	170327	1302689	2147482817	3193283
429496564	6 293773	209623		119747	85899313	82245879	784039 100547	7027 6400843		40153 40961
429496565			147827	4294965659	1745921	16582879	118757	28071671	20929	858993133
429496567	6 107374141	28825273	119557 715827613	4603393 4294965679	429496567 101873	4294965671 18013	505409	4294965673 4294965683	93368819 1360889	3011 12347
4294965680 4294965690		1431655229	488949 1753	2038427 477218411	47721841		130261	45613		7880671
429496570	6 1859439		1151	75431	42949657 61356653	3373 13267	94399 72727	13054607 2238127		
4294965710			2147482859	889411	1556147	4294965721	118273	249287	153391633	29153
4294965731	5 536870717	4254965737	179	8783161 7517	16519099	494413 130150477	1889691	4294965733 7309	2147482867 6701	859853 1553333
4294965746 4294965756	6 2147482873 6 2818219		63161261	650851	121843	225050829	29173	142837	2147482877	6270023
4294965760	6 1026031	4294965767	7877 2311	204522179 24793	1677721 7229	18755309 477218419	89669 1000691	82183 19792469	1073741441	4457 65497
4294965776 4294965786	6 268435361 6 4286393		1162687 84407	603989	4933	12377423	836573	42223	536870723	16943
4294965796	6 4337	55823	57649	1811 919	3538 21474829	41698697 7052489	102559	4294965793 556559	306783271	286331053 8753
4294965800 4294965810	6 23831 6 6761	41357 677119	24317 349241	116080157 2165893	143165527 57527	38008547 4294965821		1431655271	17471	122713309
4294965821	40829	2129	357913819	4799	38669	651641	536870729	81037091 1395829	20719	19088737
4294965836 4294965846		7883 4294965847		4294965839 1431655283	1626481 721843	4294965841 954649	21474829Z1 32749	48651	1757351	99409
4294965856	7129	237173	72211	148102271	214748293	11096103	309391	346117 4864061	4303573 25565273	733 7933
4294965866 4294965878			1073741467	33353 477218431	407879 107374147	613566553 186737647	258435367 28031	85173 70309	2147482937 1091	15959 5843491
4294965886	5 2147482943	4294965887	2179	2081903	2161	366997	6869	620929	6949783	78090289
4294965896		364591	2147482949	613566557 110127331	14316553	252645053 4294965911	2147482951 87767	9633 7829	1009 7588279	858993181 944987
4294965914	12064511	75217	167759	18481	103643	485683	25799	125941	351931	171798637
429496592 <b>1</b> 4294965936		3119 4294965937	1574401 1621	52181 130150483	181913 214748297	97553 49603	831713 639783	2243 1290167	43826183 536870743	3886847 19927
4294965946	74051137	263	3933119	4294965949	4651	79259	3947579	25718359	1494421	122713313
4294965956 4294965966		38693387 4294965967	6221 2591	138547289 8699	627919 991909	30634727 4294965971	306783283 13597	1431655321 311749	241453 1990253	858993193 457
4294965976	76695821	4294965977	.68389	1321	690509	1431655327	911	74471	91867	80513
4294965966 4294965996			25158817 33331	15259 4289	229	61333 4294966001	117709 715827667	5282861 1322749	5276371 38053	\$58993199 32497
4294966006	36398017	4294966007	178956917	60492479	13159	243769	1073741503	471301	1318263	1340083
4294966016 4294966026			415133 258173	2579 254879	5939 2225371	40031 116080163	19701679	6537239 3637	529981 358691	19219 11003
4294966036	56512711	2235797	65075243	47197429	110581	320927	93368827	4294966043	357913837	1128769
4294966046 4294966056	4519	163683 2213	134217689 2147483029	273617 59069	9544369 2788939	3256229 54366659	3343 24683713	238649 351269	126322531 28627	277363 16231
	2147483033	613566581	3224449	9695183	10475527	3853	949229	4294956073	11987	171798543
4294966086	79536409	4294966087	182129 3701	91382257 1431655363	1033	12521767	303617 357913841	46182431 1081583	7110871 8803	68791 13634813
4294966096	20543	44278001	45137	4294966099	829	85733	306783293	340573	2657	1433
4294966116		3271109	1073741527 2147483059	35083 33294311	233549 22171	4554577 4294966121	7064089 14035837	167269 2633333	69273647 1823	78990293 11453243
4294966126	2749	73583		4294966129	874249	1759	242873	665783	31122943	2340581
4294966146	1993949	340519	8873897	252645067 9697	1213 40009	1326477 8641783	580400#3 4153	792283 4294966153	4793489 2147483077	27709459 286331077
4294966156 4294966166		186737659 155801	77647 905347		53687077	5168431	288679	4294966163	578213	122713319
4294966176	481067	4294966177	74051141	251 2237	13015049	82139 390451471	16067 55063669	5661 517933	9629969 97987	171798647 86531
4294965186 4294966196	128613	4294966187	18837571 2008871	80737 7548271	119737 1022611	21367991 352133	24403217	14965039	191	365063
4294965206	1053537	2113	5162219	57847	1633067	2245147	6317 525571	18313 6719	2562629 21503	19976587 286331081
4294966216 4294966226		4294966217 894887	43481	237469	10853	1748053	30246241	1361	5263439	15618059
4294966236	1121987	4294966237	9787 95287	446323 1190071	199673 246271	4294966231 38239	536870779 23743	1739557 4294966243	4029049 1073741561	812671 15070057
4294966246 4294966256	2147483123 38347913	566693 477218473	462421	28676409	3367	1431655417	1109	116080169	763957	9323
4294966266	163543	355573	171401 1073741567	12744707 381673	13463 61356661	5501 96263	16393001 683	29671 2217329	821 2147483137	29620457 179
4294966276 4294966286	859681	87652373	715827713	2963	9761287	4673	5691	35537	58169	858993257
4294966296	304867	15391 4294966297	143779	16417 332711	2663 26141	72796039	43161269 340557	6721387 35747	74051143 1254371	37347533 40904441
4294966306 4294966316	251197	2458481	357913459	127663	919693	477218475	2753	390451483	15230377	31547
4294966326	1571	5940479 116080171	108191 536878791	6074917 159072827	5051 430789	226050859 19489	139801 174337	49367429 613566619	1600Z11 49941469	197243 397
4294966336 4294966346	17159 195225743	4294966337 68174069	1411889 77813	325697 39403361	1614649 28633109	2706343 135347	2147483171 5209	252645079	178956931	858993269
4294966356	36893	8761	2147483179	75350287	107053	146681	23091217	54133 1762399	200381 1367	856993271 25733
4294966368 4294966376	283571 26249	4294966367 1907	561029 113025431	401887 390451489	429496637 14251	1431655457	117877 108827	4294966373 159072829	170557 268435399	701219
			151637	2464123	273043	33818633	890333	1057613	126322541	73727 19991
4234966386	3851								100000	13331
4294966396 4294966406	32783	1013661	17459213 6047	399941 41698703	1342177 3407	5557 22067	48761 97612873	109001	357913867	858993281 858993283

171798691 122713351 65537

Time taken to calculate S(n) depends on how easy it is to factor n. Less time is required if n has "small" prime factors. So, in the following table, the values of n shown are the mid-points of ranges  $(n-99 \ thru \ n+99)$ . Times shown are for calculating S(n) for all integers in each range 10 times over:

n	time (ms)
100	268
200	308
400	345
800	387
1600	432
3200	490
6400	571
12800	661
25600	766
51200 102400	919
204800	2450 4036
409600	5670
819200	7977
1638400	10423
3276800	13004
6553600	16302
13107200	23438
26214400	29642
52428800	37011
104857600	50330
209715200	62363
419430400	77888
838860800	108179
1677721600	158480
3355443200	159111

"Time to n" is the time taken to calculate S(n) for all  $n \le that shown$ . "Time add." is the time taken to calculate S(n) for all n > previous n and  $\le that calculate shown is considered. All times are in milliseconds (as per version 1):$ 

John McCarthy 17 Mount Street Mansfield Notts. NG19 7AT United Kingdom

# Mike Mudge pays a return visit to the Florentin Smarandache Function <sup>1</sup>

The originator of this function. Florentin Smarandache, an Eastern European mathematician. escaped from the country of his birth because the Communist authorities had prohibited the publication of his research papers and his participation in international congresses. After spending two years in a political refugee camp in Turkey, he emigrated to the United States.

Robert Muller of The Number Theory Publishing Company, PO Box 42561, Phoenix. Arizona 85080, USA, decided to publish a selection of his papers, mmencing with The Smarandache

Function Journal, Vol 1, No 1, December 1990, ISSN 1053-4792.

PCW readers may have met this function before, in Numbers Count -112-July 1992, where a very encouraging response was generated. This article [February 1993] is complete in itself so don't worry if you have filed the July issue! It may be thought that those readers who attempted the previous problem-set will have an unfair advantage. However, it must be realised that no Numbers Count problems are completely original so previous work within a given subject area is always a possibility and the prize is awarded using 'suitable subjective criteria' anyway, so please have a go and submit your results. however trivial they may seem to vourself.

<u>Definition</u> For all non-null integers, n. the Smarandache Function, S(n), is defined to be the smallest integer such that (S(n))! (The Factorial Function with argument S(n),) is divisible by n. e.g. S(18) = 6 because 6! is divisible by 18 but 1!....5! are not.

<u>Problem (0)</u> Design and implement an algorithm to generate and store/tabulate S(n) as a function of n upto a given

Hint It may be advantageous to consider the STANDARD FORM of n. viz n = ep; p; p; p; .....p; where e=±1, and p, p, p, ...p, denote the distinct prime factors of n and a, a, a, ...a, are their respective multiplicities.

NOTE S(n) is an even function, by which is meant S(-n) = S(n).

Problem (i) Using either graphical or finite difference technique (i.e. the construction of difference tables etc) or indeed anything else that comes to mind address the following questions: (a) Is there a closed expression (formula) for S(n)?

(b) is there a good asymptotic expression for S(n)? (By which is meant a formula, which although never (in general) exact, becomes a better and better approximation to S(n) as n becomes larger and larger.)

Problem (ii) For a specified non-null integer m, under what conditions does S(n) divide the difference n - m?

<u>Problem (iii)</u> Investigate the possible integer solutions, (x,y,z) of  $S(x^a) + S(y^n) = S(z^a)$  for any n greater than or equal to 1. e.g. examine the solution (5.7,2048) when n = 3.

(It can be proved that an infinity of solutions exist for any such n-value.) Compare with Fermat's Theorem re.  $x^a+y^a=z^a$ .

<u>Problem (iv)</u> Investigate the possibility of finding two integers n and k such that the LOGARITHM of S(n\*) to the BASE S(k\*) is an integer.

Problem (v) Recall that 'Gamma' defined as the limit as n tends to infinity of (1 + 1/2 + 1/3 + 1/4....+1/n - log(n)) exists, is known as Euler's Constant and is approximately 0.577.

Investigate the possible existence of 'Samma' defined as the limit as n tends to infinity of  $(1 + 1/S(2) + 1/S(3)....+1/S(n) - \log(S(n))$ .

Problem (vi) Find the number of PAR-TITIONS of n as the sum of S(m) for 2<m≤n. See PCW August 1989 and February 1990 for other problems involving PARTITIONS of n. Review of 'Numbers Count -118-February 1993: a revisit to The Florentin Smarandache Function<sup>2</sup> This produced a number of 'quite powerful' responses. As a note of related interest, the latest publication of Fl.Smarandache is 'A Numerical Function in Congruence Theory', Libertas Mathematica (American Romanian Academy of Arts and Science) vol 12, 1992, pp 181-185, Arlington, Texas.

Pal Gronas of Norway submitted theoretical results on both problems 0 & (v). However, the clear winner this month is a former regular respondent, now retired, Henry Ibstedt, Glimminge 2036, 280 60 Broby, Sweden, Henry used a dtk-computer

with 486/33MHz processor in Borland's Turbo Basic. S(n) upto 10<sup>6</sup> took 2hr 50min. He completed a great deal of work on all

problems except (vi): details of numerical results and conclusions available from Henry or myself to interested readers. What about problem (vi)?

Republished from <Personal Computer World>, No.118, 403, February 1993 (with the author permission), because some of the following research papers are referring to these open problems.

<sup>2</sup>Republished from <Personal Computer World>, No.124, 495, August
1993 (with the author permission).

## A NOTE ON S (pr)

by Pål Grønås Enges Gate 12 7500 STaøRDAL Norway

**Problem (0).** If  $\prod_{i=1}^k p_i^{r_i}$  is the prime factorization of n, then it is easy to verify that

$$S(n) = S(\prod_{i=1}^{k} p_i^{r_i}) = \max\{S(p_i^{r_i})\}_{i=1}^{k}.$$

From this formula we see that it is essensial to determine  $S(p^r)$ , where p is a prime and r is a natural number.

Legendres formula states that

$$n! = \prod_{i=1}^k p_i^{\sum_{m=1}^{\infty} [n/p_i^m]}.$$

This formula gives us a lower and an upper bound for  $S(p^r)$ , namely

$$(1) (p-1)r+1 \leq S(p^r) \leq pr.$$

It also implies that p divides  $S(p^r)$ , which means that

$$S(p^r) = p(r-i)$$
 for a particular  $0 \le i \le [\frac{r-1}{p}]$ .

# A proof of the non-existence of "Samma".

by Pål Grønås

<u>Introduction</u>: If  $\prod_{i=1}^k p_i^{r_i}$  is the prime factorization of the natural number  $n \geq 2$ , then it is easy to verify that

$$S(n) = S(\prod_{i=1}^{k} p_i^{r_i}) = \max\{ S(p_i^{r_i}) \}_{i=1}^{k}.$$

From this formula we see that it is essential to determine  $S(p^r)$ , where p is a prime and r is a natural number.

Legendres formula states that

(1) 
$$n! = \prod_{i=1}^{k} p_i^{\sum_{m=1}^{\infty} [n/p_i^m]}.$$

The definition of the Smarandache function tells us that  $S(p^r)$  is the least natural number such that  $p^r \mid (S(p^r))!$ . Combining this definition with (1), it is obvious that  $S(p^r)$  must satisfy the following two inequalities:

(2) 
$$\sum_{k=1}^{\infty} \left[ \frac{S(p^r) - 1}{p^k} \right] < r \leq \sum_{k=1}^{\infty} \left[ \frac{S(p^r)}{p^k} \right].$$

This formula (2) gives us a lower and an upper bound for  $S(p^r)$ , namely

$$(3) (p-1)r + 1 \le S(p^r) \le pr.$$

It also implies that p divides  $S(p^r)$ , which means that

$$S(p^r) = p(r-i)$$
 for a particular  $0 \le i \le \left[\frac{r-1}{p}\right]$ .

"Samma": Let  $T(n) = 1 - \log(S(n)) + \sum_{i=2}^{n} \frac{1}{S(i)}$  for  $n \geq 2$ . I intend to prove that  $\lim_{n \to \infty} T(n) = \infty$ , i.e. "Samma" does not exist.

First of all we define the sequence  $p_1 = 2$ ,  $p_2 = 3$ ,  $p_3 = 5$  and  $p_n =$  the nth prime.

Next we consider the natural number  $p_m^n$ . Now (3) gives us that

since S(k) > 0 for all  $k \ge 2$ ,  $p_a^b \le p_m^n$  whenever  $a \le m$  and  $b \le n$  and  $p_a^b = p_c^d$  if and only if a = c and b = d.

Furthermore  $S(p_m^n) \leq p_m n$ , which implies that  $-\log S(p_m^n) \geq -\log(p_m n)$  because  $\log x$  is a strictly increasing function in the intervall  $[2,\infty)$ . By adding this last inequality and (4), we get

since both  $\sum_{k=1}^t \frac{1}{k}$  and  $\sum_{k=1}^t \frac{1}{p_k}$  diverges as  $t \to \infty$ . In other words,  $\lim_{n \to \infty} T(n) = \infty$ .  $\square$ 

## A BASIC PROCedure to calculate S(p^i)

by John Sutton 16A Overland Rd. Mumbles, SWANSEA SA3 4LP, U. K.

Integer function of a single variable S%(N%)

S is the least integer such that S! is divisible by N.

Obviously for a prime S(p)=p since this is the least factorial to include p.

It is easy to see that for two primes p1>p2 S(p1\*p2)=p1 since this factorial is necessary to include p1 and already includes p2. This generalizes to the product of any number of primes.

In fact it generalizes to the product of relatively prime numbers nl and n2. S(n1\*n2)=Max(s(n1),S(n2)).

Therefore we can simplify the general case to:

S(Ini^pi) =Max(S(ni^pi))

All we need now is a way of calculating S for powers of primes.

Start with the inverse problem: for a given factorial and a given prime what is the maximum power of the prime included?

Consider p=2. All even numbers contribute a factor, all multiples of 4 contribute another, all multiples of 8 contribute yet another ...etc. So the answer is got by summing succesive DIV 2 results (DIV p in general).

Returning to the calculation of S. To do this for a single N would require factorisation of N first. A program to calculate S for all integers up to N can avoid this by doing powers of 2, then powers of 3 and their products with powers of 2 then powers of 5 etc. Calculating S for all powers of a prime up to a maximum is straightforward. A BASIC PROCedure is attached. The main program requires some care and I have not been able to finish in time.

```
10REM TEST PROC TOCALC S(P^I) FOR VALUES UPTO N
 20:
 30:
 40:
 50:
 60INPUT"UP TO", N%
 70DIM SPP%(100)
 80DIM NPP%(100)
 90INPUT"WHICH PRIME", P%
100PROCSpp(P%,N%)
110FOR I%=0 TO 100
120PRINT SPP%(I%), NPP%(I%)
130NEXT I%
140GOTO 60
150END
160DEF PROCSpp(P%,N%)
1701%=1
180NPP%(0)=1
190SPP%(0)=1
200J%=1
210PJ%=0
220REPEAT
230PJ%=PJ%+P%
240X%=FNinvSpp(P%,PJ%)
250REPEAT
260SPP%(I%)=PJ%
270NPP%(I%)=P%*NPP%(I%-1)
2801%=1%+1
290UNTIL 1%>X%
300J%=J%+1
310UNTIL NPP%(I%-1)>N%
320ENDPROC
330DEF FNinvSpp(P%,N%)
340LOCAL S%, T%
3505%=0
360T%=N%
370REPEAT
380T%=T% DIV P%
3905%=5%+T%
400UNTIL T%<=1
410=S%
```

Henry Ibstedt Glimminge 2036 280 60 Broby Sweden

### The Florentin Smarandache Function S(n)

#### PCW February 1993

#### Problem (0)

A program SMARAND has been designed to generate S(n) up to a preset limit N (N up to 1000000 has been used in some applications). The program requires an input of prime number up to  $\sqrt{N}$ . Initially the program caculates  $S(p_i^k) = D(i,k)$  for all primes  $p_i$  and all exponents k needed to reach the preset limit. It then proceeds to factorize consecutive values of n. If n is prime then S(n) = n otherwise  $p_i^k$  is replaced by D(i,k) whenever k > 1. The largest component in the resulting array is determined and is equal to S(n). Slighly different versions of the program has been used depending on the application. Up to n = 32000 both S(n) and D(i,k) were registed on files. The values of S(n) for  $n \le 4800$  were listed with the help of a program SN TAB and the values of  $S(p_i^k)$  were listed for  $p_i \le 73$ ,  $k \le 75$  with the help of a program SN TAB.

### Problem (i)

- (a) No closed expression for S(n) has been found
- (b) No asymptotic expression for S(n) has been found. The behaviour of S(n) for  $n \le 32000$  has been graphically displayed using a program  $SN\_DISTR$ .

#### Problem (ii)

S(n)/(n-m),  $m \neq 0$  is equivalent to

$$m=n+kS(n)$$
, k integer .... (1)

Let us assume that m is a given prime p. From the definition of S(n) it is evident that for every n there exists a prime q such that q/n (or n=lq, l integer) and S(n)=jq (i integer). We can therefore write (1) in the form

$$p = q(1+kj) ... (2)$$

To find solutions to (1) when m is a prime p it is therefore sufficient to chose n as a multiple of p which fills the condition l+kj=1.

In practice (as far as I have found) this means excluding from n those multiples of m(=p) which are divisible by primes larger than p and also cases where n-m has a different parity from S(n) as for example (n,m,S(n))=(5054,19,38) is not a solution while (2527,29,38) is a

solution.

When m is not a prime let p be the largest prime such that p/m, i.e. m=rp. Solutions to (1) will then be found when n is a multipe of p for which the GCD of n and S(n) is rp.

The above conditions are sufficient but may not be necessary. Lists of solutions are however easily obtained (not included) by looking for solutions to (n-m) mod S(n) = 0.

#### Problem (iii)

A number of solutions to  $S(x^n) + S(y^n) = S(z^n)$  has been obtained and listed for n = 3,5,7 and 11. The program  $SMAR_{iii}$  uses only Smarandache function values of the type  $S(p_i^k)$  which had first been sorted in ascending order using a program SNP SORT.

## Problem (iv)

A program  $SMAR_iv$  has been designed to find solutions to the equation  $S(k^n)^i = S(n^k)$  but no non-trivial solutions were found in the selected search area  $n \le 8000$ .

#### Problem (v)

In a first attempt values saved on file up to 32000 were in a program  $SMAR_{\nu}$  to calculate the sums Z(n)=1+1/S(2)+1/S(3)+...+1/S(n) for n=800, 1600, 2400, ... 32000. These sums were used to study the behaviour of Z(n)-T(n) for various functions T(n):

T(n) = log(S(n)) gave a curve "parallel" to Z(n).

 $T(n) = \log(\text{largest prime} < n)$  gave a similar result.

 $T(n) = 1 + 1/2^a + 1/3^a + ... + 1/n^a$  gave interesting results. Supplemented with a linear term a "nearly straight horizontal" line was obtained.

To see if this holds for larger values the exercise was repeated for  $n \le 1000000$ . Computer files to store S(n) is now out of question and the generating program SMARAND was revised so that the partial sums Z(n) were calculated in the same program. T(n) was calculated in a separate program for vaious values of a. For a = 0.5 and it was found that

$$1+1/S(2)+1/S(3)+...+1/S(n)-(1+1/\sqrt{2}+1/\sqrt{3}+...+1/\sqrt{n})-(20k-58)$$

where k = n/25000 deviates from 0 with at most 10 in the interval 1 to 1000000 (at the points of representations in the graph, 1000000 was divided in 40 interval of 25000).

#### Problem (vi)

Not attempted.

#### **Equipment**

Calculations were done on an dtk-computer with 486/33 Mhz processor. Programs were written in Borlands Turbo Basic. Printouts were done on an HP IIP Laser printer. Some graphs were done on an HP Paintjet. The run time to calculate S(n) up to 1000000 was 2 h 50 m. The initial calculation up 32767 took 198 s.

#### 'SMARAND, H. Ibstedt, 930320

The Smarandache function S(n) calculated by comparing largest prime and  $S(P^A)$ . The values of S(n) are calculated and registered in a file SN.DAT up to n=32000. The calculation goes further in other applications.

DEFLNG A-S CLS:T=TIMER DIM P(168),D(168,75),K(168),L(168) OPEN "PA" FOR INPUT AS #1 FOR I=1 TO 168:INPUT #1,P(I):NEXT:CLOSE #1

This part of the program calculates  $S(P(I)^A)$  and saves the result in the array D(I,A), P(I) is the lth prime number. The routine uses the fact that  $D(I,A) < = P(I)^*A$  for a downward search for the value of D(I,A). This calculation goes beyond what is required to calculate S(n) up to n=32000.

```
FOR I=1 TO 42
A=2:P=P(1):D(1,1)=P
WHILE A < 76
C=0:N=0
 L:
C=C+1
N = N + P
IF C> = A THEN D(I,A) = N : GOTO LWEND
PP=P*P
 L1:
IF N-PP*INT(N/PP) = 0 THEN C=C+1:PP=PP*P:GOTO L1
IF C> = A THEN D(I,A) = N : GOTO LWEND : ELSE L
 LWEND:
INCR A
WEND
NEXT
```

'The array D(I.A) is stored in a file SNP.DAT for future use.

OPEN "SNP.DAT" FOR OUTPUT AS #2 FOR I=1 TO 42 :FOR J=1 TO 75 PRINT #2,P(I),J,D(I,J) NEXT :NEXT :CLOSE #2

This part of the program calculates S(N). It calls on the subroutine NFACT to express N in prime factor form. Factors  $P(I)^A$  with A > 1 are replaced by D(I,A) and placed in array L(I) together with the factors P(I) of multiplicity 1. S(N) is stored in a file SN.DAT.

N=1
OPEN "SN.DAT" FOR APPEND AS #3
WRITE #3,1
WHILE N<32000
INCR N :print n
'Factorize N.

```
GOSUB NFACT
IF K(0) > 0 THEN S = P(0) : GOTO LWR
'Construct L().
 FOR I=1 TO 168:L(I)=0:NEXT
 C = 0
 FOR I=1 TO M
INCR C
IF K(I) = 1 THEN L(C) = P(I)
IF K(I) > 1 THEN L(C) = D(I, K(I))
NEXT
'Find the largest value of L() and hence S(N).
S=0
FOR I=1 TO C
IF L(I) > S THEN S = L(I)
NEXT
 LWR:
WRITE #3.S
WEND
CLOSE #3
T=TIMER-T:PRINTT
'Subroutine for factorization of N.
 NFACT:
FOR I=0 TO 168 :K(I)=0 :NEXT :P(0)=0
N1 = N : M = 0
FOR I=1 TO 168
 LA:
IF N1-P(I)*INT(N1/P(I)) = 0 THEN K(I) = K(I) + 1 : M = I : N1 = N1/P(I) : GOTO LA
IF N1 = 1 THEN I = 168
NEXT
IF N1 > 1 THEN P(0) = N1 : K(0) = 1
RETURN
```

#### 'SN TAB, H. Ibstedt, 930321

This program uses the results stored in the file SN.DAT produced by the program SMARAND to tabulate the first 4800 values of the function S(N).

'Set I = 21 and NB = 82 on HPIIP.

```
DEFINT I-P.S:DIM S(4800)
CLS: WIDTH "LPT1:".120:S(1)=1:T=TIMER
OPEN "SN.DAT" FOR INPUT AS #1
FOR I=1 TO 4800
INPUT #1.S(I)
NEXT
CLOSE #1
            " :S2$="-
                               S4$=" n | S(n) | ":S5$=" n | S(n) | ":S6$=" n | S(n) | "
       _# :83$=#_
11 = 1 : 12 = 75 : P1 = 1
LW:
LPRINT TAB(8) "The Smarandache Function S(n).
LPRINT TAB(8) S1$; :FOR I=1 TO 6 :LPRINT S2$; :NEXT :LPRINT S3$;
LPRINT TAB(8) S4$: :FOR I=1 TO 6 :LPRINT S5$; :NEXT :LPRINT S6$;
LPRINT TAB(8) $7$: :FOR I=1 TO 6 :LPRINT $8$: :NEXT :LPRINT $9$:
FOR I=11 TO 12
LPRINT TAB(8) "":
FOR J=0 TO 7
LPRINT USING "#####";I+J*75; :LPRINT "°"; :LPRINT USING "#####";S(I+J*75);
LPRINT " ":
NEXT
NEXT
LPRINT TAB(8) B1$; :FOR I=1 TO ■:LPRINT B2$; :NEXT :LPRINT B3$;
LPRINT TAB(8) "Page"P1 "of 8.
LPRINT CHR$(12)
IF P1 = 1 THEN P1 = 2: I1 = 601: I2 = 675: GOTO LW
IF P1 = 2 THEN P1 = 3 : I1 = 1201 : I2 = 1275 : GOTO LW
IF P1 = 3 THEN P1 = 4: I1 = 1801: I2 = 1875: GOTO LW
IF P1 = 4 THEN P1 = 5 : I1 = 2401 : I2 = 2475 : GOTO LW
IF P1 = 5 THEN P1 = 6: I1 = 3001: I2 = 3075: GOTO LW
IF P1 = 6 THEN P1 = 7: I1 = 3601: I2 = 3675: GOTO LW
IF P1 = 7 THEN P1 = 8:11 = 4201:12 = 4275:GOTO LW
PRINT "END" :END
```

n	S(n)	n	\$(n)	n	S(n)	n	S(n)	n	S(n)	n	S(n)	n	S(n)	n	S(n)
1	0	76	19	151	151	226	113	301	43	376	47	451	41	526	263
2 3	2	77	11	152 153	19	227 228	227	302 303	151	377 378	29	452 453	113	527 528	31
4	4	79	79	154	11	229	229	304	19	379	379	454	227	529	46
5	5	80	6	155	31	230	23	305	61	380	19	455	13	530	53
6 7	3 7	81 82	41	156 157	157	231	11 29	306 307	17 307	381 382	127 191	456 457	19 457	531 532	59 19
8	4	83	83	158	79	233	233	308	11	383	383	458	229	533	41
9	6	84	7	159	53	234	13	309	103	384	8	459	17	534	89
10 11	5 11	85 86	17 43	160	8 23	235 236	47 59	310 311	31 311	385 386	11 193	460 461	23 461	535 536	107
12	4	87	29	162	9	237	79	312	13	387	43	462	11	537	179
13	13	88	11	163	163	238	17	313	313	388	97	463	463	538	269
14	7	89 90	89	164	41	239 240	239	314 315	157 7	389 390	389 13	464	29 31	539 540	14
16	6	91	13	166	83	241	241	316	79	391	23	466	233	541	541
17	17	92	23	167	167	242	22	317	317	392	14	467	467	542	271
18 19	19	93 94	31 47	168	7 26	243 244	12 61	318 319	53 29	393 394	131 197	468 469	13 67	543 544	181
20	5	95	19	170	17	245	14	320	8	395	79	470	47	545	109
21 22	7	96 97	97	171	19 43	246	41	321	107	396 397	11 397	471	157 59	546 547	13
23	11 23	98	14	172 173	173	247 248	19 31	322 323	23 19	398	199	472 473	43	548	547 137
24	4	99	11	174	29	249	83	324	9	399	19	474	79	549	61
25	10 13	100 101	101	175 176	10	250 251	15 251	325	13 163	400 401	10 401	475	19	550 551	11
26 27	9	102	17	177	11 59	252	7	326 327	109	402	67	476	53	552	29 23
28	7	103	103	178	89	253	23	328	41	403	31	478	239	553	79
29 30	29 5	104 105	13	179 180	179 6	254 255	127 17	329 330	47 11	404 405	101	479 480	479 8	554 555	277 37
31	31	106	53	181	181	256	10	331	331	406	29	481	37	556	139
32	8	107	107	182	13	257	257	332	83	407	37	482	241	557	557
33 34	11 17	108 109	9 109	183 184	61 23	258 259	43 37	333 334	37 167	408 409	17 409	483 484	23 22	558 559	31 43
35	7	110	11	185	37	260	13	335	67	410	41	485	97	560	7
36	6	111	37	186	31	261	29	336	7	411	137	486	12	561	17
37 38	37 19	112 113	7 113	187 188	17 47	262 263	131 263	337 338	337 26	412 413	103 59	487 488	487 61	562 563	281 563
39	13	114	19	189	9	264	11	339	113	414	23	489	163	564	47
40	5	115	23	190	19	265	53	340	17	415	83	490	14	565	113
41	41	116 117	29 13	191 192	191	266 267	19 <b>89</b>	341 342	31 19	416 417	13 139	491 492	491 41	566 567	283 9
43	43	118	59	193	193	268	67	343	21	418	19	493	29	568	71
44	11	119	17	194	97	269	269	344	43	419	419	494	19	569	569
45 46	6 23	120 121	5 22	195 196	13 14	270 271	9 271	345 346	23 173	420 421	7 421	495 496	11 31	570 571	19 571
47	47	122	61	197	197	272	17	347	347	422	211	497	71	572	13
48	6	123	41	198	11	273	13	348	29	423	47	498	83	573	191
49 50	14 10	124 125	31 15	199 200	199	274 275	137 11	349 350	349 10	424 425	53 17	499 500	499 15	574 575	41 23
51	17	126	7	201	67	276	23	351	13	426	71	501	167	576	8
52 53	13 53	127 128	127 8	202	101	277 278	277 139	352 353	11	427 428	61 107	502 503	251 503	577 578	577 34
54	9	129	43	203	29 17	279	31	354	353 59	429	13	504	7	579	193
55	11	130	13	205	41	280	7	355	71	430	43	505	101	580	29
56 57	7	131 132	131 11	206 207	103 23	281 282	281 47	356 357	89 17	431 432	431 9	506 507	23 26	581 582	83 97
58	29	133	19	208	13	283	283	358	179	433	433	508	127	583	53
59	59	134	67	209	19	284	71	359	359	434	31	509	509	584	73
60 61	5 61	135 136	9 17	210 211	7 211	285 286	19 13	360 361	6 38	435 436	29 109	510 511	17 73	585 586	13 293
62	31	137	137	212	53	287	41	362	181	437	23	512	12	587	587
63	7	138	23	213	71	288	8	363	22	438	73	513	19	588	14
64	8	139 140	139 7	214 215	107 43	289 290	34 29	364 365	13 73	439 440	439 11	514 515	257 103	589 590	31 59
66	11	141	47	216	9	291	97	366	61	441	14	516	43	591	197
67	67	142	71	217	31	292	73	367	367	442	17	517	47	592	37 507
68 69	17 23	143	13	218 219	109 73	293 294	293	368 369	23 41	443	443 37	518 519	37 173	59 <b>3</b> 594	593 11
70	7	145	29	220	11	295	59	370	37	445	89	520	13	595	17
71 72	71	146	73	221	17	296	37	371	53	446	223	521 522	521	596	149
16		147	14	222	37	297	11	372	31	447	149	522	29	597	199
73	73	148	37	223	223	298	149	373	373	448	8	523	523	598	23
		148 149 150	37 149 10	223 224 225	223 8 10	298 299 300	23 10	374 375	17 15	449 450	449 10	524 525	131	598 599 600	23 599 10

			101 3(11												
n	S(n)	n	S(n)	n	S(n)	n	S(n)	п	S(n)	n	\$(n)	n	S(n)	n	S(n)
601	601	676	26	751	751	826	59	901	53	976	61	1051	1051	1126	563
602	43	677	677	752	47	827	827	902	41	977	977	1052	263	1127	23
603	151	678 679	113	753 754	251 29	828 829	23 829	903	113	978 979	163	1053	13	1128	47
605	22	680	17	755	151	830	83	905	181	980	14	1054	211	1129 1130	1129 113
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616	11	691	691	766	383	841	58	916	229	991	991	1066	41	1141	163
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1263 1264		1338 1339	223 103	1413 1414	157 101	1488 1489	31 1489	1563 1564	521 23	1638 1639	13 149	1713 1714	571 957	1788	149
1265		1340	67	1415	283	1490	149	1565	313	1640	41	1715	857 21	1789 1790	1789 179
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n	S(n)	n	S(n)	n	\$(n)	п	S(n)	n	\$(n)	n	S(n)	n	S(n)	n	S(n)
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2402	1201	2477	2477	2552 2553	29 37	2627 2628	71 73	2702 2703	193 53	2777 2778	2777 463	2852 2853	31 317	2927 2928	2927 61
2403	<b>89</b> 601	2478 2479	67	2554	1277	2629	239	2704	26	2779	397	2854	1427	2929	101
2405	37	2480	31	2555	73	2630	263	2705	541	2780	139	2855	571	2930	293
2406	401	2481	827	2556	71	2631	877	2706	41	2781	103	2856	17	2931	977
2407	83 43	2482 2483	73 191	2557 2558	2557 1279	2632 2633	47 2633	2707 2708	2707 677	2782 2783	107 23	2857 2858	2857 1429	2932 2933	733 419
2408	*3 73	2484	23	2559	853	2634	439	2709	43	2784	29	2859	953	2934	163
2410	241	2485	71	2560	12	2635	31	2710	271	2785	557	2860	13	2935	587
2411	2411	2486	113	2561	197	2636	659	2711	2711	2786	199	2861	2861	2936	367
2412	67	2487	829	2562	61	2637 2638	293	2712 2713	113 2713	2787 2788	929 41	2862 2863	53 409	2937 2938	89 113
2413	127 71	2488 2489	311 131	2563 2564	233 641	2639	1319 29	2714	59	2789	2789	2864	179	2939	2939
2415	23	2490	83	2565	19	2640	11	2715	181	2790	31	2865	191	2940	14
2416	151	2491	53	2566	1283	2641	139	2716	97	2791	2791	2866	1433	2941	173
2417	2417	2492	89	2567	151	2642	1321 881	2717 2718	19 151	2792 2793	349 19	2867 2868	61 239	2942 2943	1471
2418	31 59	2493 2494	277 43	2568 2569	107 367	2643 2644	661	2719	2719	2794	127	2869	151	2944	23
2420	22	2495	499	2570	257	2645	46	2720	17	2795	43	2870	41	2945	31
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2424	97	2500	20	2575	103	2650	53	2725	109	2800	10	2875	23	2950	59
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2444	47 163	2519 2520	229 7	2594 2595	1297 173	2669 2670	157 89	2744 2745	21 61	2819 2820	2819 47	2894 2895	1447 193	2970	11
2446	1223	2521	2521	25%	59	2671	2671	2746	1373	2821	31	2896	181	2971	2971
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2450 2451	14 43	2525 2526	421	2601	34	2676	223	2751	131	2826	157	2901	967	2976	31
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2454	409	2529 2530	281 23	2604 2605	31 521	2679 2680	47 67	2754 2755	17 29	2829 2830	41 283	2904 2905	22 83	2979 2980	331 149
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2457					79	2682	149	2757	919	2832	59	2907	19	2982	71
2458	13	2532	211	2607						2833	2833	2908	727	2983	157
2459	1229	2533	149	2608	163	2683	2683	2758	197		:				
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\$\frac{5}{500}   \$\frac{7}{7}   \$\frac{5}{307}   \$\frac{1}{181}   \$3152   \$\frac{1}{97}   \$322   \$461   \$3302   \$173   \$337   \$307   \$352   \$843   \$327   \$323   \$305   \$317   \$307   \$307   \$315   \$431   \$322   \$269   \$3303   \$357   \$358   \$269   \$3305   \$260   \$3305   \$260   \$3505   \$260	<b>—</b>			<del> </del>	+	1	-	-	-	-	-	-	-	-	-	
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3074 53 3149 67 3224 31 3299 3299 3374 241 3449 3449 3524 881 3599 61	3072	12	3147	1049	3222	179	3297	157	3372	281	3447	383	3522	587	3597	109
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300 10 360 10 360 10 300 11 3300 13 300 10																
	3013	71	3130	10	360	*3	2200		3313	13	J-30	ے	3763	*1	3000	10

Page 6 of 8.

п	S(n)	n	\$(n)	n	S(n)	n	\$(n)	n	S(n)	п	S(n)	n	S(n)	n	S(n)
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3602	1801	3677	3677	3752	67	3827 3828	89	3902	1951	3977	97	4052	1013	4127	4127
3603 3604	1201	3678 3679	613 283	3753 3754	139	3829	29 547	3903 3904	1301	3978 3979	173	4053 4054	193	4128 4129	4129
3605	103	3680	23	3755	751	3830	383	3905	71	3980	199	4055	811	4130	59
3606	601	3681	409	3756	313	3831	1277	3906	31	3981	1327	4056	26	4131	17
3607 3608	3607	3682 3683	263	3757	34	3832 3833	479	3907	3907	3982	181	4057	4057	4132	1033
3609	401	3684	127 307	3758 3759	1879	3834	3833 71	3908 3909	977	3983 3984	569 83	4058 4059	2029	4133 4134	4133
3610	38	3685	67	3760	47	3835	59	3910	23	3985	797	4060	29	4135	827
3611	157	3686	97	3761	3761	3836	137	3911	3911	3986	1993	4061	131	4136	47
3612	43	3687	1229	3762	19	3837	1279	3912	163	3987	443	4062	677	4137	197
3613 3614	3613 139	3688 3689	461	3763 3764	71 941	3838 3839	101 349	3913 3914	103	3988 3989	997 3989	4063 4064	239 127	4138 4139	2069 4139
3615	241	3690	41	3765	251	3840	10	3915	29	3990	19	4065	271	4140	23
3616	113	3691	3691	3766	269	3841	167	3916	89	3991	307	4066	107	4141	101
3617	3617	3692	71	3767	3767	3842	113	3917	3917	3992	499	4067	83	4142	109
3618 3619	67 47	3693 3694	1231	3768 3769	157 3769	3843 3844	61	3918 3919	653 3919	3993 3994	1997	4068 4069	113 313	4143	1381
3620	181	3695	739	3770	29	3845	769	3920	14	3995	47	4070	37	4145	829
3621	71	3696	11	3771	419	3846	641	3921	1307	3996	37	4071	59	4146	691
3622	1811	3697	3697	3772	41	3847	3847	3922	53	3997	571	4072	509	4147	29
3623 3624	3623 151	3698 3699	86 137	3773 3774	21 37	3848 3849	37 1283	3923 3924	3923 109	3998 3999	1999	4073	4073	4148 4149	61 461
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3626	37	3701	3701	3776	59	3851	3851	3926	151	4001	4001	4076	1019	4151	593
3627	31	3702	617	3777	1259	3852	107	3927	17	4002	29	4077	151	4152	173
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3630	22	3705	19	3780	9	3855	257	3930	131	4005	89	4080	17	4155	277
3631	3631	3706	109	3781	199	3856	241	3931	3931	4006	2003	4081	53	4156	1039
3632	227	3707	337	3782	61	3857	29	3932	983	4007	4007	4082	157	4157	4157
3633 3634	173	3708 3709	103 3709	3783 3784	97	3858 3859	643 227	3933 3934	23 281	4008 4009	167 211	4083 4084	1361 1021	4158 4159	11 4159
3635	727	3710	53	3785	757	3860	193	3935	787	4010	401	4085	43	4160	13
3636	101	3711	1237	3786	631	3861	13	3936	41	4011	191	4086	227	4161	73
3637	3637	3712	29	3787	541	3862	1931	3937	127	4012	59	4087	67	4162	2081
3638 3639	107	3713 3714	619	3788 3789	947 421	3863 3864	3863 23	3938 3939	179 101	4013 4014	4013 223	4088 4089	73 47	4163 4164	181 347
3640	13	3715	743	3790	379	3865	773	3940	197	4015	73	4090	409	4165	17
3641	331	3716	929	3791	223	3866	1933	3941	563	4016	251	4091	4091	4166	2083
3642	607	3717	59	3792	79	3867	1289	3942	73	4017	103	4092	31	4167	463
3643 3644	3643 911	3718 3719	26 3719	3793 3794	3793 271	3868 3869	967 73	3943 3944	3943 29	4018 4019	41 4019	4093 4094	4093 89	4168 4169	521 379
3645	15	3720	31	3795	23	3870	43	3945	263	4020	67	4095	13	4170	139
3646	1823	3721	122	3796	73	3871	79	3946	1973	4021	4021	4096	16	4171	97
3647	521	3722	1861	3797	3797	3872	22	3947	3947	4022	2011	4097	241	4172	149
3648 3649	19 89	3723 3724	73 19	3798 3799	211 131	3873 3874	1291 149	3948 3949	47 359	4023 4024	149 503	4098 4099	683 4099	4173 4174	107 20 <b>8</b> 7
3650	73	3725	149	3800	19	3875	31	3950	79	4025	23	4100	41	4175	167
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3652	83	3727	3727	3802	1901	3877	3877	3952	19	4027	4027	4102	293	4177	4177
3653 3654	281 29	3728 3729	233 113	3803 3804	3803 317	3878 3879	277 431	3953 3954	67 659	4028 4029	53 79	4103 4104	373 19	4178 4179	2089 199
3655	43	3730	373	3805	761	3880	97	3955	113	4030	31	4105	821	4180	19
3656	457	3731	41	3806	173	3881	3881	3956	43	4031	139	4106	2053	4181	113
3657	53 50	3732	311	3807	47 17	3882	647	3957	1319	4032	8	4107	74 70	4182	41 80
3658 3659	59 3659	3733 3734	3733 1867	3808 3809	17 293	3883 3884	353 971	3958 3959	1979 107	4033 4034	109 2017	4108 4109	79 587	4183 4184	89 523
3660	61	3735	83	3810	127	3885	37	3960	11	4035	269	4110	137	4185	31
3661	523	3736	467	3811	103	3886	67	3961	233	4036	1009	4111	4111	4186	23
3662	1831	3737	101	3812	953	3887	26	3962	283	4037	367	4112	257 (57	4187	79 7/0
3663 3664	37 229	3738 3739	89 3739	3813 3814	41 1907	3888 3889	12 3889	3963 3964	1321 991	4038 4039	673 577	4113 4114	457 22	4188 4189	349 71
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3666	47	3741	43	3816	53	3891	1297	3966	661	4041	449	4116	21	4191	127
3667	193	3742	1871	3817	347	3892	139	3967	3967	4042	47	4117	179	4192	131
3668 3669	131 1223	3743 3744	197 13	3818 3819	83 67	3893 3894	229 59	3968 3969	31 14	4043 4044	311 337	4118 4119	71 1373	4193 4194	599 233
3670	367	3745	107	3820	191	3895	41	3970	397	4045	809	4120	103	4195	839
3671	3671	3746	1873	3821	3821	3896	487	3971	38	4046	34	4121	317	4196	1049
3672	17	3747	1249	3822	14	3897	433	3972	331	4047	71	4122	229	4197	1399
3673 3674	3673 167	3748 3749	937 163	3823 3824	3823 239	3898 3899	1949 557	3973 3974	137 1987	4048 4049	23 4049	4123 4124	31 1031	4198 4199	2099 19
	14	3750	20	3825	17	3900	13	3975	53	4050	10	4125	15	4200	10
3675							1		1						

0	S(n)	n	\$(n)	n	S(n)	l n	S(n)	n	S(n)	n	S(n)	n	S(n)	n	S(n)
4201	4201	4276	1069	4351	229	4426	2213	4501	643	4576	13	4651	4651	4726	139
4202	191	4277	47	4352	17	4427	233	4502	2251	4577	199	4652	1163	4727	163
4203 4204	1051	4278 4279	31 389	4353 4354	1451	4428 4429	41	4503	79	4578	109	4653	47	4728	197
4205	58	4280	107	4355	67	4430	103	4504 4505	563 53	4579 4580	241	4654 4655	179	4729 4730	4729 43
4206	701	4281	1427	4356	22	4431	211	4506	751	4581	509	4656	97	4731	83
4207 4208	601 263	4282 4283	2141 4283	4357	4357	4432	277	4507	4507	4582	79	4657	4657	4732	26
4209	61	4284	17	4358 4359	2179 1453	4433 4434	739	4508 4509	167	4583 4584	4583	4658	137 1553	4733 4734	4733 263
4210	421	4285	857	4360	109	4435	887	4510	41	4585	131	4660	233	4735	947
4211 4212	4211	4286 4287	2143	4361	89	4436	1109	4511	347	4586	2293	4661	79	4736	37
4213	383	4288	67	4362 4363	727 4363	4437 4438	317	4512	4513	4587 4588	139	4662 4663	37 4663	4737 4738	1579
4214	43	4289	4289	4364	1091	4439	193	4514	61	4589	353	4664	53	4739	677
4215 4216	281 31	4290 4291	613	4365	97	4440	37	4515	43	4590	17	4665	311	4740	79
4217	4217	4292	37	4366 4367	59 397	4441	2221	4516 4517	1129 4517	4591 4592	4591	4666 4667	2333	4741 4742	431 2371
4218	37	4293	53	4368	13	4443	1481	4518	251	4593	1531	4668	389	4743	31
4219 4220	4219	4294	113 859	4369	257	4444	101	4519	4519	4594	2297	4669	29	4744	593
4221	67	4295 4296	179	4370 4371	23 47	4445	127	4520 4521	113	4595 4596	919 383	4670	173	4745	73
4222	2111	4297	4297	4372	1093	4447	4447	4522	19	4597	4597	4672	73	4747	113 101
4223	103	4298	307	4373	4373	4448	139	4523	4523	4598	22	4673	4673	4748	1187
4224 4225	11 26	4299 4300	1433	4374	18	4449 4450	1483	4524 4525	29 181	4599 4600	73 23	4674	17	4749 4750	1583
4226	2113	4301	23	4376	547	4451	4451	4526	73	4601	107	4676	167	4751	19 4751
4227	1409	4302	239	4377	1459	4452	53	4527	503	4602	59	4677	1559	4752	11
4228 4229	151 4229	4303 4304	331 269	4378	199	4453 4454	73 131	4528 4529	283 647	4603	4603	4678	2339	4753	97
4230	47	4305	41	4380	73	4455	11	4530	151	4604 4605	1151 307	4679 4680	4679	4754 4755	2377 317
4231	4231	4306	2153	4381	337	4456	557	4531	197	4606	47	4681	151	4756	41
4232 4233	83	4307 4308	73 359	4382 4383	313 487	4457 4458	4457	4532	103	4607	271	4682	2341	4757	71
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4238	163	4313	227	4388	107	4462 4463	97 4463	4537 4538	349 2269	4612 4613	1153 659	4687 4688	109 293	4762 4763	2381 433
4239	157	4314	719	4389	19	4464	31	4539	89	4614	769	4689	521	4764	397
4240 4241	53 4241	4315 4316	863	4390 4391	439 4391	4465 4466	47 29	4540	227	4615	71	4690	67	4765	953
4242	101	4317	1439	4392	61	4467	1489	4541 4542	239 757	4616 4617	577 19	4691 4692	4691	4766 4767	2383 227
4243	4243	4318	127	4393	191	4468	1117	4543	59	4618	2309	4693	38	4768	149
4244 4245	1061	4319 4320	617	4394 4395	39	4469	109	4544	71	4619	149	4694	2347	4769	251
4246	193	4321	149	4396	293 157	4470 4471	149 263	4545 4546	101 2273	4620 4621	11 4621	4695 4696	313 587	4770 4771	53 367
4247	137	4322	2161	4397	4397	4472	43	4547	4547	4622	2311	4697	61	4772	1193
4248 4249	59 607	4323	131	4398	733	4473	71	4548	379	4623	67	4698	29	4773	43
4250	17	4324 4325	47 173	4399 4400	83 11	4474	2237 179	4549 4550	4549 13	4624 4625	34 37	4699 4700	127 47	4774	31 191
4251	109	4326	103	4401	163	4476	373	4551	41	4626	257	4701	1567	4776	199
4252 4253	1063 4253	4327 4328	4327 541	4402 4403	71	4477	37	4552	569	4627	661	4702	2351	4777	281
4254	709	4328	541 37	4404	37 367	4478 4479	2239 1493	455 <b>3</b> 4554	157 23	4628 4629	89 1543	4703 4704	4703 14	4778 4779	2389 59
4255	37	4330	433	4405	881	4480	8	4555	911	4630	463	4705	941	4780	239
4256 4257	19 43	4331 4332	71 38	4406 4407	2203	4481	4481	4556	67	4631	421	4706	181	4781	683
4258	2129	4333	619	4407	113 29	4482 4483	83 4483	4557 4558	31 53	4632 4633	193 113	4707 4708	523 107	4782 4783	797 4783
4259	4259	4334	197	4409	4409	4484	59	4559	97	4634	331	4709	277	4784	23
4260	71 4241	4335	34	4410	14	4485	23	4560	19	4635	103	4710	157	4785	29
4261 4262	4261 2131	4336 4337	271 4337	4411 4412	401 1103	4486 4487	2243 641	4561 4562	4561 2281	4636 4637	61 4637	4711 4712	673 31	4786 4787	2393 4787
4263	29	4338	241	4413	1471	4488	17	4563	26	4638	773	4713	1571	4788	19
4264 4265	41	4339	4339	4414	2207	4489	134	4564	163	4639	4639	4714	2357	4789	4789
4266	853 79	4340 4341	31 1447	4415 4416	883 23	4490 4491	449	4565 4566	83 761	4640 4641	29 17	4715 4716	131	4790 4791	479 1597
4267	251	4342	167	4417	631	4492	1123	4567	4567	4642	211	4717	89	4792	599
4268	97	4343	101	4418	94	4493	4493	4568	571	4643	4643	4718	337	4793	4793
4269 4270	1423 61	4344 4345	181 79	4419 4420	491	4494	107 31	4569 4570	1523 457	4644	43 929	4719 4720	22 59	4794 4795	137
4271	4271	4346	53	4421	4421	4496	281	4571	653	4646	101	4721	4721	4796	109
4272	89	4347	23	4422	67	4497	1499	4572	127	4647	1549	4722	787	4797	41
4273 4274	4273 2137	4348 4349	1087 4349	4423	4423	4498 4499	173 409	4573 4574	269 2287	4648	4649	4723	4723	4798	2399
4275	19	4350	29	4425	59	4500	15	4575	61	4650	4649	4724 4725	1181	4799 4800	4799 10
	l							1	1						

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#### 'SNP TAB, H. Ibstedt, 930322

'This program tabulates S(n) for  $n=P^J$ , 1<P<74, 1<J.76, using data form the file SNP ASC.

```
DEFLNG I-S: DIM KP(1575).KJ(1575).SP(1575)
CLS:
WIDTH "LPT1:",120
OPEN "SNP.DAT" FOR INPUT AS #1
FOR I=1 TO 1575
INPUT #1.KP(I).KJ(I).SP(I)
NFXT
CLOSE #1
S1$=" -
                        e" :S2$="-
S4$=" P(I)
              J [D(I,J)[":S5$=" P(I)
                                         J DOLLING
57$=" L
81$="L
                          :82$="-
S3$="--
S6$=" P(I) |
                DCL_J)!"
S9$=#-
83$="-
I1 = 1:I2 = 75:P1 = 1
LW:
LPRINT TAB(12) "The Smarandache Function S(n) = D(I,J) for powers of primes P(I)^J."
LPRINT TAB(12) S1$; :FOR I=1 TO 3 :LPRINT S2$; :NEXT :LPRINT S3$;
LPRINT TAB(12) S4$: :FOR I=1 TO 3 :LPRINT S5$: :NEXT :LPRINT S6$:
LPRINT TAB(12) $7$: :FOR I=1 TO 3 :LPRINT $8$: :NEXT :LPRINT $9$:
FOR |= |1 TO |2
LPRINT TAB(12) "I":
FOR J=0 TO 4
LPRINT USING "#####":KP(I+J*75):
LPRINT " | "; :LPRINT USING "#####";KJ(I+J*75); :LPRINT " | "; :LPRINT USING
"#####":SP(I+J*75);
LPRINT" I":
NEXT
NEXT
LPRINT TAB(12) B1$: :FOR I = 1 TO 3 :LPRINT B2$: :NEXT :LPRINT B3$:
LPRINT TAB(12) "Page"P1 "of 3.
LPRINT CHR$(12)
IF P1=1 THEN P1=2:I1=601:I2=675:GOTO LW
IF P1 = 2 THEN P1 = 3: 11 = 1201: 12 = 1275: GOTO LW
PRINT "END" :END
```

2 1 2 3 1 1 3 5 5 1 1 5 7 1 1 7 11 1 1 1 1 2 2 2 2 2 4 4 3 3 2 6 5 5 2 10 7 7 2 14 11 1 2 2 2 2 3 4 3 3 4 3 3 9 5 3 11 5 7 3 2 11 1 1 3 33 3 1 2 2 4 6 6 3 3 4 9 5 5 4 20 7 7 4 28 11 1 4 44 44 44 44 44 44 44 44 44 44 44	The Smar	randach	e Funct	ion S(n)	)=0(1,3	) for po	wers of	prime	s P(1) J	4					
2	P(1)	J	0(1,1)	P(1)	J	0(1,1)	P(I)	1	D(I,J)	P(1)	J	0(1,1)	P(I)	1	(L,I)
2   3	2											1 (			
2	2														
2	2														44
2 2 21 24 3 21 45 5 21 90 7 21 133 11 21 22 231 2 2 24 3 5 22 48 5 5 22 95 7 22 140 11 21 22 231 22 24 28 3 22 48 5 5 24 100 7 24 147 11 23 242 242 2 2 26 28 3 245 54 5 24 100 7 24 147 11 23 242 24 2 2 2 26 28 3 2 25 54 5 54 5 25 105 7 25 154 11 26 264 24 2 2 2 2 25 28 3 2 25 54 5 52 54 100 7 24 147 11 12 24 242 24 2 2 2 25 28 3 2 25 54 5 52 54 105 7 25 154 11 26 264 11 1 26	2			3		: 1	5		25	7					
2 2 21 24 3 21 45 5 21 90 7 21 133 11 21 22 231 2 2 24 3 5 22 48 5 5 22 95 7 22 140 11 21 22 231 22 24 28 3 22 48 5 5 24 100 7 24 147 11 23 242 242 2 2 26 28 3 245 54 5 24 100 7 24 147 11 23 242 24 2 2 2 26 28 3 2 25 54 5 54 5 25 105 7 25 154 11 26 264 24 2 2 2 2 25 28 3 2 25 54 5 52 54 100 7 24 147 11 12 24 242 24 2 2 2 25 28 3 2 25 54 5 52 54 105 7 25 154 11 26 264 11 1 26	2												r .		
2 2 21 24 3 21 45 5 21 90 7 21 133 11 21 22 231 2 2 24 3 5 22 48 5 5 22 95 7 22 140 11 21 22 231 22 24 28 3 22 48 5 5 24 100 7 24 147 11 23 242 242 2 2 26 28 3 245 54 5 24 100 7 24 147 11 23 242 24 2 2 2 26 28 3 2 25 54 5 54 5 25 105 7 25 154 11 26 264 24 2 2 2 2 25 28 3 2 25 54 5 52 54 100 7 24 147 11 12 24 242 24 2 2 2 25 28 3 2 25 54 5 52 54 105 7 25 154 11 26 264 11 1 26	2				ŀ										
2 2 21 24 3 21 45 5 21 90 7 21 133 11 21 22 231 2 2 24 3 5 22 48 5 5 22 95 7 22 140 11 21 22 231 22 24 28 3 22 48 5 5 24 100 7 24 147 11 23 242 242 2 2 26 28 3 245 54 5 24 100 7 24 147 11 23 242 24 2 2 2 26 28 3 2 25 54 5 54 5 25 105 7 25 154 11 26 264 24 2 2 2 2 25 28 3 2 25 54 5 52 54 100 7 24 147 11 12 24 242 24 2 2 2 25 28 3 2 25 54 5 52 54 105 7 25 154 11 26 264 11 1 26	2										-	1 1			
2 2 21 24 3 21 45 5 21 90 7 21 133 11 21 22 231 2 2 24 3 5 22 48 5 5 22 95 7 22 140 11 21 22 231 22 24 28 3 22 48 5 5 24 100 7 24 147 11 23 242 242 2 2 26 28 3 245 54 5 24 100 7 24 147 11 23 242 24 2 2 2 26 28 3 2 25 54 5 54 5 25 105 7 25 154 11 26 264 24 2 2 2 2 25 28 3 2 25 54 5 52 54 100 7 24 147 11 12 24 242 24 2 2 2 25 28 3 2 25 54 5 52 54 105 7 25 154 11 26 264 11 1 26	2				1							63	,		110
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P(I)	J	D(1,1)	P(I)	J	(1,1)	P(I)	J	D(1,1)	P(I)	J	(1,1)0	P(I)	J	(L, I)
23	1 2	23	29 29	1 2	29 58	31 31	1 2	31 62	37 37	1 2	37 74	41 41	1	41
23	3	69	29	3	87	31	3	93	37	3	111	41	3	82 123
23	4	92	29	4	116	31	4	124	37	4	148	41	4	164
23	5	115	29	5	145	31	5	155	37	5	185	41	5	205
23	6 7	138	29 29	6 7	174	31 31	6 7	186 217	37 37	6 7	222	41	6 7	246 287
23	8	184	29	8	232	31	8	248	37	8	296	41	8	328
23	9	207	29	9	261	31	9	279	37	9	333	41	9	369
23 23	10	230 253	29 29	10	290 319	31 31	10	310 341	37 37	10	370 407	41	10	410
23	12	276	29	12	348	31	12	372	37	12	444	41	12	492
23	13	299	29	13	377	31	13	403	37	13	481	41	13	533
23 23	14	322 345	29 29	14	406 435	31 31	14	434 465	37 37	14	518 555	41	14	574 615
23	16	368	29	16	464	31	16	496	37	16	592	41	16	656
23	17	391	29	17	493	31	17	527	37	17	629	41	17	697
23 23	18 19	414	29 29	18 19	522 551	31 31	18	558 589	37 37	18	666 703	41 41	18	738 779
23	20	460	29	20	580	31	20	620	37	20	740	41	19	820
23	21	483	29	21	609	31	21	651	37	21	777	41	21	861
23	22	506	29	22	638	31	22	682	37	22	814	41	22	902
23 23	23 24	529 529	29 29	23 24	667 696	31 31	23	713 744	37 37	23 24	851 888	41 41	23	943 984
23	25	552	29	25	725	31	25	775	37	25	925	41	25	1025
23	26	575	29	26	754	31	26	806	37	26	962	41	26	1066
23	27 28	598 621	29 29	27 28	783 812	31 31	27 28	837 868	37 37	27 28	999 1036	41 41	27 28	1107 1148
23	29	644	29	29	841	31	29	899	37	29	1073	41	29	1189
23	30	667	29	30	841	31	30	930	37	30	1110	41	30	1230
23 23	31 32	690 713	29 29	31 32	870 899	31 31	31 32	961 961	37 37	31 32	1147 1184	41	31 32	1271 1312
23	33	736	29	33	928	31	33	992	37	33	1221	41	33	1353
23	34	759	29	34	957	31	34	1023	37	34	1258	41	34	1394
23 23	35 36	782 805	29 29	35 36	986 1015	31 31	35 36	1054 1085	37 37	35 36	1295 1332	41 41	35 36	1435 1476
23	37	828	29	37	1044	31	37	1116	37	37	1369	41	37	1517
23	38	851	29	38	1073	31	38	1147	37	38	1369	41	38	1558
23 23	39 40	874 897	29 29	39 40	1102 1131	31 31	39 40	1178 1209	37 37	39 40	1406 1443	41 41	39 40	1599 1640
23	41	920	29	41	1160	31	41	1240	37	41	1480	41	41	1681
23	42	943	29	42	1189	31	42	1271	37	42	1517	41	42	1681
23 23	43	966 989	29 29	43 44	1218 1247	31 31	43 44	1302 1333	37 37	43 44	1554 1591	41	43	1722 1763
23	45	1012	29	45	1276	31	45	1364	37	45	1628	41 41	45	1804
23	46	1035	29	46	1305	31	46	1395	37	46	1665	41	46	1845
23 23	47 48	1058 1058	29	47 48	1334 1363	31 31	47	1426	37	47	1702	41	47	1886
23	49	1038	29 29	49	1392	31	48 49	1457 1488	37 37	48 49	1739 1776	41 41	48 49	1927 1968
23	50	1104	29	50	1421	31	50	1519	37	50	1813	41	50	2009
23	51	1127	29	51	1450	31	51	1550	37	51	1850	41	51	2050
23	52 53	1150 1173	29 29	52 53	1479 1508	31 31	52 53	1581 1612	37 37	52 53	1887 1924	41 41	52 53	2091 2132
23	54	1196	29	54	1537	31	54	1643	37	54	1961	41	54	2173
23	55	1219	29	55	1566	31	55	1674	37	55	1998	41	55	2214
23	56 57	1242 1265	29 29	56 57	1595 1624	31 31	56 57	1705 1736	37 37	56 57	2035 2072	41	56 57	2255 2296
23	58	1288	29	58	1653	31	58	1767	37	58	2109	41	58	2337
23	59	1311	29	59	1682	31	59	1798	37	59	2146	41	59	2378
23	60 61	1334 1357	29 29	60 61	1682 1711	31 31	60 61	1829 1860	37 37	60 61	2183 2220	41 41	60 61	2419 2460
23	62	1380	29	62	1740	31	62	1891	37	62	2257	41	62	2501
23	63	1403	29	63	1769	31	63	1922	37	63	2294	47-	63	2542
23 23	64	1426 1449	29 29	64 65	1798 1827	31 31	64 65	1922 1953	37 37	64 65	2331 2368	41.	64 65	2583 2624
23	66	1472	29	66	1856	31	66	1984	37	66	2405	41	66	2665
23	67	1495	29	67	1885	31	67	2015	37	67	2442	41	67	2706
23 23	68 69	1518 1541	29 29	68 69	1914 1943	31	68 69	2046 2077	37 37	68 69	2479 2516	41	68 69	2747 2788
23	70	1564	29	70	1972	31	70	2108	37	70	2553	41	70	2829
23	71	1587	29	71	2001	31	71	2139	37	71	2590	41	71	2870
23 23	72 73	1587 1610	29 29	72 73	2030	31	72	2170 2201	37 37	72	2627 2664	41	72	2911 2952
23	74	1633	29	74	2088	31	74	2232	37	74	2701	41	74	2993
23	75	1656	29	75	2117	31	75	2263	37	75	2738	41	75	3034

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59         11         649         61         11         671         67         11         737         71         11         781         73           59         12         708         61         12         732         67         12         804         71         12         852         73           59         14         826         61         14         854         67         14         938         71         14         994         73           59         15         885         61         15         915         67         15         1005         71         15         1065         73           59         16         944         61         16         976         67         15         1005         71         15         1065         73           59         17         1003         61         17         1037         67         17         113         71         17         120         1342         73           59         18         1062         61         18         1098         67         18         1206         71         18         1278         73         73         79	1 73 2 146 3 219
59         3         177         61         3         183         67         3         201         71         3         213         73           59         4         236         61         4         244         67         4         268         73           59         6         354         61         6         366         67         6         402         71         6         426         73           59         6         354         61         6         366         67         7         469         71         7         497         73         75         79         7         497         73         73         79         639         73         73         79         639         73         73         79         639         73         79         639         73         79         639         73         79         67         79         607         71         10         70         70         71         70         70         71         71         71         71         73         73         73         73         73         73         73         73         73         73         73	
59         4         236         61         4         244         67         4         268         71         4         284         73           59         5         295         61         5         305         67         5         335         71         5         355         73           59         6         354         61         6         366         67         7         469         71         7         497         73           59         7         413         61         7         427         67         7         469         71         7         497         73           59         8         472         61         8         488         67         8         536         71         9         639         73           59         10         590         61         10         610         67         10         670         71         10         710         73           59         11         649         61         11         671         67         11         73         71         11         710         71         11         710         71         71         7	
59         5         295         61         5         305         67         5         335         71         5         355         73           59         6         354         61         6         366         67         6         402         71         6         426         73           59         8         472         61         8         488         67         8         536         71         3         568         73           59         9         531         61         9         549         67         9         603         71         9         639         73         79         639         73         79         639         73         79         639         73         79         639         73         79         639         73         79         639         73         79         639         73         79         639         73         79         639         73         79         639         73         79         637         71         10         710         73         73         79         73         73         73         79         637         71         11         73	292
59         7         413         61         7         427         67         7         469         71         7         497         73           59         8         472         61         8         488         67         8         536         71         8         568         73           59         10         590         61         10         610         67         9         603         71         9         639         73           59         11         649         61         11         671         11         737         71         11         73         73           59         12         708         61         12         752         67         12         804         71         12         852         73           59         12         708         61         12         752         67         12         804         71         12         852         73         73         75         99         12         885         61         13         793         67         13         871         71         13         993         73         73         73         73         73	365
59         8         472         61         8         488         67         8         536         71         8         568         73           59         9         531         61         9         549         67         9         603         71         9         639         73           59         10         590         61         11         671         67         10         670         71         19         639         73           59         11         649         61         11         671         67         11         737         71         11         781         73           59         12         708         61         13         793         67         12         804         71         12         852         73           59         13         885         61         15         915         67         15         1005         71         15         1065         73           59         16         944         61         16         976         67         15         1005         71         15         1065         73           59         18         1062 </td <td>438</td>	438
599         9         531         61         9         549         67         9         603         71         9         639         73           599         10         590         61         10         610         67         11         670         71         10         710         73           599         11         649         61         12         732         67         12         804         71         12         852         73           599         13         767         61         13         793         67         13         871         71         13         923         73           599         14         826         61         15         915         67         13         871         71         13         923         73           599         16         944         61         16         976         67         15         1005         71         15         1065         73           599         16         944         61         16         976         67         17         1139         71         17         1207         73           599         16	7 511 8 584
59         10         590         61         10         610         67         10         670         71         10         710         73           59         11         649         61         11         671         67         11         737         71         11         781         73           59         12         708         61         12         732         67         12         804         71         12         852         73           59         13         767         61         13         793         67         13         804         71         12         852         73           59         14         826         61         14         854         67         14         938         71         14         994         73           59         15         885         61         15         915         67         15         1005         71         15         1065         73           59         16         944         61         16         976         67         16         1007         71         15         1065         73         17         17         130	657
59         11         649         61         11         671         67         11         737         71         11         781         73           59         12         708         61         12         732         67         12         804         71         12         852         73           59         13         767         61         13         793         67         13         871         71         13         923         73           59         14         826         61         14         854         67         14         938         71         14         994         73           59         15         885         61         15         915         67         15         1005         71         15         1065         73           59         16         944         61         16         976         67         16         1072         71         16         1136         73           59         18         1062         61         18         1098         67         18         1206         71         18         1278         73         73         73         73	730
59         12         708         61         12         732         67         12         804         71         12         852         73           59         13         767         61         13         793         67         13         871         71         13         923         73           59         14         826         61         14         854         67         14         938         71         14         994         73           59         15         885         61         15         915         67         15         1005         71         15         1065         73           59         16         944         61         16         976         67         16         1072         71         16         1136         73           59         18         1062         61         18         1098         67         18         1206         71         18         1277         73         73           59         11         120         61         21         1281         67         21         1407         71         21         1491         73         73         73	1 803
59         14         826         61         14         854         67         14         938         71         14         994         73           59         15         885         61         15         915         67         15         1005         71         15         1065         73           59         16         944         61         16         976         67         16         1072         71         16         1136         73           59         17         1003         61         17         1037         67         17         1139         71         16         1136         73           59         18         1062         61         18         1098         67         18         1206         71         18         1278         73           59         19         1121         61         19         1159         67         19         1273         71         19         1349         73           59         20         1180         61         20         1220         67         20         1340         71         20         1420         73           59         21	2 876
59         15         885         61         15         915         67         15         1005         71         15         1065         73           59         16         944         61         16         976         67         16         1072         71         16         1136         73           59         17         1003         61         17         1037         67         17         1139         17         120         73           59         18         1062         61         18         1098         67         18         1206         71         18         1278         73           59         19         1121         61         19         1159         67         19         1273         71         19         1349         73           59         20         1180         61         20         1220         67         20         1340         71         20         1420         73           59         21         1239         61         21         1281         67         21         1407         71         21         1420         73           59         21 <td< td=""><td>949</td></td<>	949
59         16         944         61         16         976         67         16         1072         71         16         1136         73           59         17         1003         61         17         1037         67         17         1139         71         17         1207         75           59         18         1062         61         18         1098         67         18         1206         71         18         1278         73           59         19         1121         61         19         1159         67         19         1233         71         19         1349         73           59         20         1180         61         20         1220         67         20         1340         71         20         1420         73           59         21         1239         61         21         1281         67         21         1407         71         21         1491         73           59         22         1298         61         22         1342         67         22         1474         71         22         1562         73           59	4 1022 5 1095
59         17         1003         61         17         1037         67         17         1139         71         17         1207         73           59         18         1062         61         18         1098         67         18         1206         71         18         1278         73           59         19         1121         61         19         1159         67         19         1273         71         19         1349         73           59         20         1180         61         20         1220         67         20         1340         71         20         1420         73           59         21         1239         61         21         1281         67         20         1340         71         20         1420         73           59         22         1298         61         22         1342         67         22         1474         71         22         1562         73           59         22         1298         61         23         1403         67         23         1541         71         24         1704         73         24         1640	6 1168
59         18         1062         61         18         1098         67         18         1206         71         18         1278         73           59         19         1121         61         19         1159         67         19         1273         71         19         1349         73           59         20         1180         61         20         1220         67         20         1340         71         20         1420         73           59         21         1239         61         21         1281         67         21         1407         71         21         1491         73           59         22         1298         61         22         1342         67         22         1474         71         22         1562         73           59         23         1357         61         23         1403         67         23         1541         71         23         1633         73           59         24         1416         61         24         1464         67         24         1608         71         24         1704         75           59	7 1241
59         19         1121         61         19         1159         67         19         1273         71         19         1349         73           59         20         1180         61         20         1220         67         20         1340         71         20         1420         73           59         21         1239         61         21         1281         67         21         1407         71         21         1491         73           59         22         1298         61         22         1342         67         22         1474         71         22         1562         73           59         23         1357         61         23         1403         67         23         1541         71         23         1633         73           59         24         1416         61         24         1464         67         24         1608         71         24         1704         75           59         25         1475         61         25         1526         67         25         1675         71         25         1775         73         25         1675	1314
59         20         1180         61         20         1220         67         20         1340         71         20         1420         73           59         21         1239         61         21         1281         67         21         1407         71         21         1491         73           59         22         1298         61         22         1342         67         22         1474         71         21         1491         73           59         23         1357         61         23         1403         67         23         1541         71         23         1633         73           59         24         1416         61         24         1464         67         24         1608         71         24         1704         75           59         25         1475         61         25         1525         67         25         1675         71         25         1775         73           59         26         1534         61         26         1586         67         26         1742         71         26         1846         73         27         1917	9   1387
59         22         1298         61         22         1342         67         22         1474         71         22         1562         73           59         23         1357         61         23         1403         67         23         1541         71         23         1633         73           59         24         1416         61         24         1464         67         24         1608         71         24         1704         73           59         26         1534         61         25         1525         67         25         1675         71         26         1846         73           59         26         1534         61         26         1586         67         26         1742         71         26         1846         73           59         27         1593         61         27         1647         67         27         1809         71         27         1917         73           59         28         1652         61         28         1708         67         28         1876         71         28         1988         73           59	0 1460
59         23         1357         61         23         1403         67         23         1541         71         23         1633         73           59         24         1416         61         24         1464         67         24         1608         71         24         1704         73           59         25         1475         61         25         1525         67         25         1675         71         25         1775         73           59         26         1534         61         26         1586         67         26         1742         71         26         1846         73           59         27         1593         61         27         1647         67         27         1809         71         27         1917         73           59         28         1652         61         28         1708         67         29         1943         71         29         2059         73           59         30         1770         61         30         1830         67         30         2010         71         30         2130         73           59	1 1533 2 1606
59         24         1416         61         26         1466         67         24         1608         71         24         1704         73           59         25         1475         61         25         1525         67         25         1675         71         25         1775         73           59         26         1534         61         26         1586         67         26         1742         71         26         1846         73           59         27         1593         61         27         1647         67         27         1809         71         27         1917         73           59         28         1652         61         28         1708         67         28         1876         71         28         1988         73           59         29         1711         41         29         1769         67         29         1943         71         29         2059         73           59         30         1770         61         30         1830         67         30         2010         71         30         2130         75           59	2   1606 3   1679
59         25         1475         61         25         1525         67         25         1675         71         25         1775         73           59         26         1534         61         26         1586         67         26         1742         71         26         1846         73           59         27         1593         61         27         1647         67         27         1809         71         27         1917         73           59         28         1652         61         28         1708         67         28         1876         71         28         1988         75           59         29         1711         III         29         1769         67         29         1943         71         29         2059         73           59         30         1770         61         30         1830         67         30         2010         71         30         2130         73           59         31         1829         61         31         1891         67         31         2077         71         31         2201         73           59	4 1752
59         26         1534         61         26         1586         67         26         1742         71         26         1846         73           59         27         1593         61         27         1647         67         27         1809         71         27         1917         73           59         28         1652         61         28         1708         67         28         1876         71         28         1988         73           59         29         1711         III         29         1769         67         29         1943         71         29         2059         73           59         30         1770         61         30         1830         67         30         2010         71         30         2130         75           59         31         1829         61         31         1891         67         31         2077         71         31         2201         73           59         32         1888         61         32         1952         67         32         2144         71         32         2272         73           59	1825
59         27         1593         61         27         1647         67         27         1809         71         27         1917         73           59         28         1652         61         28         1708         67         28         1876         71         28         1988         73           59         29         1711         III         29         1769         67         29         1943         71         29         2059         73           59         30         1770         61         30         1830         67         30         2010         71         30         2130         73           59         31         1829         61         31         1891         67         31         2077         71         31         2201         73           59         32         1888         61         32         1952         67         32         2144         71         32         22772         73           59         34         2006         61         34         2074         67         34         2278         71         33         2414         73           59	6 1898
59         28         1652         61         28         1708         67         28         1876         71         28         1988         73           59         29         1711         III         29         1769         67         29         1943         71         29         2059         73           59         30         1770         61         30         1830         67         30         2010         71         30         2130         73           59         31         1829         61         31         1891         67         31         2077         71         31         2201         73           59         32         1888         61         32         1952         67         32         2144         71         32         2277         73           59         33         1947         61         33         2013         67         33         2211         71         33         2343         73           59         34         2006         61         34         2074         67         34         2278         71         34         2414         75           59	7 1971
59         30         1770         61         30         1830         67         30         2010         71         30         2130         73           59         31         1829         61         31         1891         67         31         2077         71         31         2201         73           59         32         1888         61         32         1952         67         32         2144         71         32         2272         73           59         33         1947         61         33         2013         67         33         2211         71         33         2343         75           59         34         2006         61         34         2074         67         34         2278         71         34         2414         73           59         35         2065         61         35         2135         67         35         2345         71         35         2485         73           59         36         2124         61         36         2196         67         36         2412         71         36         2556         73           59	8 2044
59         31         1829         61         31         1891         67         31         2077         71         31         2201         73           59         32         1888         61         32         1952         67         32         2144         71         32         2272         75           59         33         1947         61         33         2013         67         33         2211         71         33         2343         75           59         34         2006         61         34         2074         67         34         2278         71         34         2414         73           59         35         2065         61         35         2135         67         35         2345         71         34         2414         73           59         36         2124         61         36         2196         67         36         2412         71         36         2556         73           59         37         2183         61         37         2257         67         37         2479         71         37         2627         73           59	9 2117
59     32     1888     61     32     1952     67     32     2144     71     32     2272     73       59     33     1947     61     33     2013     67     33     2211     71     33     2343     75       59     34     2006     61     34     2074     67     34     2278     71     34     2414     73       59     35     2065     61     35     2135     67     35     2345     71     35     2485     73       59     36     2124     61     36     2196     67     36     2412     71     36     2556     73       59     37     2183     61     37     2257     67     37     2479     71     37     2627     73       59     38     2242     61     38     2318     67     38     2546     71     38     2698     73       59     39     2301     61     39     2379     67     39     2613     71     39     2697     73       59     40     2360     61     40     2440     67     40     2680     71     40 <td< td=""><td></td></td<>	
59         33         1947         61         33         2013         67         33         2211         71         33         2343         73           59         34         2006         61         34         2074         67         34         2278         71         34         2414         73           59         35         2065         61         35         2135         67         35         2345         71         35         2485         73           59         36         2124         61         36         2196         67         36         2412         71         36         2556         73           59         37         2183         61         37         2257         67         37         2479         71         37         2627         73           59         38         2242         61         38         2318         67         38         2546         71         38         2698         73           59         39         2301         61         39         2379         67         39         2613         71         49         2840         73           59	2 2336
59         34         2006         61         34         2074         67         34         2278         71         34         2414         73           59         35         2065         61         35         2135         67         35         2345         71         35         2485         73           59         36         2124         61         36         2196         67         36         2412         71         36         2556         73           59         37         2183         61         37         2257         67         37         2479         71         37         2627         73           59         38         2242         61         38         2318         67         39         2546         71         38         2698         73           59         39         2301         61         39         2379         67         39         2643         71         39         2769         73           59         40         2360         61         40         2440         67         40         2680         71         40         2840         73           59	3 2409
59     35     2065     61     35     2135     67     35     2345     71     35     2485     73       59     36     2124     61     36     2196     67     36     2412     71     36     2556     73       59     37     2183     61     37     2257     67     37     2479     71     37     2627     73       59     38     2242     61     38     2318     67     38     2546     71     38     2698     73       59     39     2301     61     39     2379     67     39     2613     71     39     2769     73       59     40     2360     61     40     2440     67     40     2680     71     40     2840     73       59     41     2419     61     41     2501     67     41     2767     71     41     2911     73	4 2482
59     36     2124     61     36     2196     67     36     2412     71     36     2556     73       59     37     2183     61     37     2257     67     37     2479     71     37     2627     73       59     38     2242     61     38     2318     67     38     2546     71     38     2698     73       59     39     2301     61     39     2379     67     39     2613     71     39     2769     73       59     40     2360     61     40     2440     67     40     2680     71     40     2840     73       59     41     2419     61     41     2501     67     41     2747     71     41     2911     73	5 2555
59     38     2242     61     38     2318     67     38     2346     71     38     2698     73       59     39     2301     61     39     2379     67     39     2613     71     39     2769     75       59     40     2360     61     40     2440     67     40     2680     71     40     2840     73       59     41     2419     61     41     2501     67     41     2747     71     41     2911     73	6 2628
59     39     2301     61     39     2379     67     39     2613     71     39     2769     73       59     40     2360     61     40     2440     67     40     2680     71     40     2840     73       59     41     2419     61     41     2501     67     41     2747     71     41     2911     73	7 2701
59 40 2360 61 40 2440 67 40 2680 71 40 2840 73 59 41 2419 61 41 2501 67 41 2747 71 41 2911 73	8 2774 9 2847
59 41 2419 61 41 2501 67 41 2747 71 41 2911 73	0 2920
27 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	1 2993
34 : 45   5410   91   45   506   91   45   5014   11   45   514	2 3066
59 43 2537 61 43 2623 67 43 2881 71 43 3053 73	3 3139
37 4 230 01 7 200 01 12 21 13 13 13 13 13	4 3212
37 43 2033 07 43 270 07 17 27 27 27 27 27 27 27 27 27 27 27 27 27	5 3285 6 3358
37 40 27 14 01 10 2000 0	7 3431
	8 3504
59 49 2891 61 49 2989 67 49 3283 71 49 3479 73	9 3577
59 50 2950 61 50 3050 67 50 3350 71 50 3550 73	0 3650
37 31 3007 81 31 311 91 31 311	1 3723
37 30 300 1 7 30 300 1	2 3796 3 3869
	4 3942
	5 4015
59 56 3304 61 56 3416 67 56 3752 71 56 3976 73	6 4088
59 57 3363 61 57 3477 67 57 3819 71 57 4047 73	7 4161
77 70 500 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	8 4234 9 4307
37 37 3401 01 37 337 01 31 31 31 31	9   4307 0   4380
	1 4453
37 01 3340 01 01 01 01 01 01 01	2 4526
59 63 3658 61 63 3782 67 63 4221 71 63 4473 73	3 4599
59 64 3717 61 64 3843 67 64 4288 71 64 4544 73	4 4672
59 65 3776 61 65 3904 67 65 4355 71 65 4615 73	5 4745
37 00 300 01 12 12 12 12 12 12 12 12 12 12 12 12 12	6   4818 7   4891
37 07 3074 01 01 100 100 100 100 100 100 100 100	8 4964
	9 5037
	0 5110
59 71 4130 61 71 4270 67 71 4690 71 71 5041 73	1 5183
59 72 4189 61 72 4331 67 72 4757 71 72 5041 73	2 5256
59 73 4248 61 73 4392 67 73 4824 71 73 5112 73	3 5329
37   70   7301   07   17   170   17   17   17   17	4 5329 5 5402
59 75 4366 61 75 4514 67 75 4958 71 75 5254 73	2   JTUG

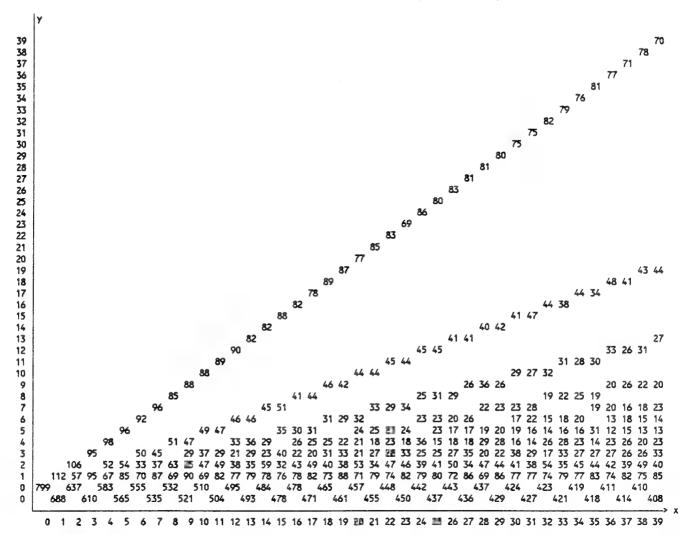
#### 'SN DISTR, H. Ibstedt, 930322

'The values of S(n) for n < 32000 are input from the file SN.DAT and the number of values falling into each square of a 40 x 40 matrix are counted and displayed in a graph. An interresting pattern is formed by large primes while the bottom layer mainly resulting form composite numbers requires two lines in the graph.

```
'Set I = 1021 and NB = 82 on HPIIP
DEFLNG A-S
DIM C(51.51)
CLS:WIDTH "LPT1:".130
LPRINT TAB(50) "The Smarandache function S(n)"
                                       - IPRINT -LPRINT
LPRINT TAB(50) "-
LPRINT TAB(35) "Number of values of S(n) in the interval 800y \mu S(n) < 800(y+1).
LPRINT
LPRINT TAB(4)" | V"
LPRINT TAB(4)" | "
OPEN "SN.DAT" FOR INPUT AS #1
WHILE K<32000
INCR K
INPUT #1.S
I=K\800+1:J=S\800+1
C(I,J) = C(I,J) + 1
WEND
CLOSE #1
FOR J = 40 TO 2 STEP -1 :LPRINT USING "###";J-1; :LPRINT " | ";
FOR I=1 TO 40
IF C(I,J) = 0 THEN LPRINT SPC(3); ELSE LPRINT USING "###";C(I,J);
NEXT:LPRINT
NEXT
LPRINT USING "###":J-1: :LPRINT " | ":
J=1:FOR I=1 TO 39 STEP 2
LPRINT USING "###";C(I,J); :LPRINT SPC(3);
NEXT:LPRINT
LPRINT USING "###";J-1; :LPRINT " | ";
FOR I=2 TO 40 STEP 2
LPRINT SPC(3); :LPRINT USING "###";C(I,J);
NEXT:LPRINT
LPRINT TAB(5) "L"; :FOR I=1 TO 120 :LPRINT "-"; :NEXT :LPRINT "> x"
LPRINT TAB(6); :FOR I=0 TO 39:LPRINT USING "###";I; :NEXT :LPRINT
LPRINT :LPRINT TAB(5) "Intervals: 800x \le n < 800(x+1).
LPRINT: LPRINT TAB(5) "SN DISTR "DATE$
LPRINT CHR$(12)
END
```

#### The Smarandache function S(n)

Number of values of S(n) in the interval  $800y \le S(n) < 800(y+1)$ .



Intervals:  $800x \le n < 800(x+1)$ .

SN\_DISTR 03-24-1993

#### 'SNP SORT, H. Ibstedt, 930322

'This program inputs the Smarandache function S(n) for powers of primes from the file SNP.DAT, sorts S(n) in ascending order and writes the result to a file SNP ASC

**DEFLNG A-S** CLS DIM D(42,75), KP(3150), KJ(3150), SP(3150) OPEN "SNP.DAT" FOR INPUT AS #1 FOR I=1 TO 42 :FOR J=1 TO 75 INCR L INPUT #1,K1,K2,K3 KP(L) = K1 : KJ(L) = K2 : SP(L) = K3**NEXT:NEXT** FOR I = 1 TO L : FOR J = I + 1 TO L - 1 IF SP(I) > SP(J) THEN SWAP SP(I), SP(J) :SWAP KJ(I), KJ(J) :SWAP KP(I), KP(J)**NEXT:NEXT** OPEN "SNP ASC" FOR OUTPUT AS #2 FOR I=1 TO L PRINT #2,KP(I),KJ(I),SP(I) **NEXT** CLOSE #2 PRINT "END" :END

#### 'SMAR III, H. Ibstedt, 930322

This program searches for solutions to  $S(x^n) + s(y^n) = S(z^n)$ . Two parameters are set in the program: n = NM and the largest value of  $S(z^n) = NS$ . x, y and z are restricted to powers of prime numbers. The input to the program is provided by the file  $SNP\_ASC$ , which contains  $S(p^n)$  sorted in ascending order.

```
DEFLNG A-P: DEFDBL X.Y.Z
 CLS:WIDTH "LPT1:",120
 DIM D(42,75),K1(3150),K2(3150),K3(3150)
 NM=3:NS=120:L=0
 OPEN "SNP ASC" FOR INPUT AS #1
 WHILE NOT EOF(1)
 INCR L: INPUT #1,K1(L),K2(L),K3(L)
 WEND:CLOSE #1:COUNT=0
 LPRINT TAB(16) "Solutions to S(x^n) + S(y^n) = S(z^n) for n = NM
 LPRINT TAB(16) :LPRINT
LPRINT TAB(16) :LPRINT * P1 | P3 |
                                                        1
                                                                      ı
                                                               y
                                                                              z
 [ S(x*n) | S(y*n) | S(z*n) |*
LPRINT TAB(16) :LPRINT
FOR I = NS TO 4 STEP -1 : PRINT I
 IF K2(I) MOD NM <> 0 THEN III
FOR J=I-1 TO 3 STEP -1
IF K2(J) MOD NM <> 0 THEN JJJ
FOR K=J-1 TO 2 STEP -1
IF COUNT = 75 THEN GOTO KKK
IF K2(K) MOD NM <> I THEN KKK
IF K1(I) = K1(J) OR K1(I) = K1(K) OR K1(J) = K1(K) THEN KKK
IF K3(1) = K3(J) + K3(K) THEN
INCR COUNT
X = K1(K)^{(K2(K)/NM)} : Y = K1(J)^{(K2(J)/NM)} : Z = K1(I)^{(K2(I)/NM)}
LPRINT TAB(16) ] "; :LPRINT USING "######":K1(K):
LPRINT " | "; :LPRINT USING "######":K1(J):
LPRINT " | "; :LPRINT USING "######";K1(I);
LPRINT "["; :LPRINT USING "###########";X;
LPRINT " | "; :LPRINT USING "############";Y;
LPRINT "|"; :LPRINT USING "############";Z;
LPRINT "!"; :LPRINT USING "#######";K3(K);
LPRINT " | "; :LPRINT USING "######";K3(J);
LPRINT " | "; :LPRINT USING "#######";K3(1);
LPRINT "I"
END IF
KKK:
NEXT
JJJ:
NEXT
111:
NEXT
LPRINT TAB(16) :LPRINT
   4 **
LPRINT CHR$(12)
PRINT "COUNT = "COUNT
PRINT "END" :END
```

5         2         3         5         32768         59049         15         48           7         2         3         7         8192         59049         24         39           5         3         2         25         243         262144         25         33           5         11         2         25         11         262144         25         33           5         7         3         5         8192         19683         15         42           7         2         3         5         8192         19683         15         42           7         2         3         7         2048         19683         24         33           5         2         3         25         1024         19683         25         32           5         2         3         25         11         19683         25         32           3         2         19         3         32768         19         9         48           2         3         19         8         2187         19         12         45           3         2         19 <th>P1</th> <th>PZ</th> <th>Р3</th> <th>х</th> <th>у</th> <th>Z</th> <th>\$(x^n)</th> <th>S(y'n)</th> <th>S(z'n)</th>	P1	PZ	Р3	х	у	Z	\$(x^n)	S(y'n)	S(z'n)
7   2   3   7   8192   59049   24   42   42   55   55   55   55   55									63
2 13 3 3 128 13 59049 24 39 5 5 11 2 2 25 265 263 262144 25 33 5 5 11 2 2 25 11 262144 25 33 5 5 7 7 3 5 5 49 19643 15 42 25 33 5 7 2048 19643 15 42 2 13 3 128 11 19643 24 33 15 42 2 11 3 128 11 19643 24 33 15 2 2 3 2 5 122 19643 25 32 2 11 3 128 11 19643 25 32 2 12 13 13 128 11 19643 25 32 2 12 13 13 128 11 19643 25 32 2 19 3 3 25 512 19643 25 32 2 19 3 3 2768 19 9 9 48 218 19 9 19 12 42 2 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1									63 63
\$ 11 2 25 25 263 263 263 144 25 33 5 5 1 1 2 262 144 25 33 5 15 42 15 5 7 3 5 5 49 19643 15 42 15 15 42 15 15 14 1 2 2 1 1 3 128 11 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1									63
5         11         2         25         11         262144         25         33           5         7         3         5         49         19643         15         42           7         2         3         5         8192         19643         21         36           2         11         3         128         11         19643         24         33           5         2         3         25         512         19643         25         32           5         2         3         25         512         19663         25         32           3         2         19         8         2187         19         9         48           2         3         19         8         2187         19         15         42           5         7         19         8         49         19         15         42           5         7         19         8         8192         19         15         42           5         2         19         7         2048         19         21         36           3         2         19 <t< td=""><td>5</td><td></td><td>2</td><td></td><td></td><td></td><td></td><td></td><td>58</td></t<>	5		2						58
5         2         3         5         8192         19643         15         36         21         36         21         36         21         36         21         36         21         36         22         33         25         1024         19643         26         32         33         25         512         11         19643         25         32         32         32         33         25         512         19643         25         32         32         32         32         33         25         32	5		2	25	11	262144	25	33	58
7   2   3   7   2048   19643   21   36   36   37   36   37   37   38   32   38   32   38   32   38   32   38   32   38   32   38   32   38   32   38   32   38   32   38   32   38   32   38   38									57
2 11 3 128 11 190683 24 33 3			3		8192				57
5         2         3         25         1024         19083         25         32           3         2         19         3         25         512         19083         25         32           3         19         8         2187         19         9         48           3         7         19         9         8         247         19         15         42           3         2         19         9         8         192         19         15         42           3         2         19         9         8         192         19         15         42           7         2         19         7         2048         19         21         36           2         19         128         243         19         24         33         19         24         33         19         24         33         19         24         33         19         24         33         19         21         36         42         33         19         21         36         42         23         33         20         10         24         33         33         20         <									57 57
5         2         3         25         512         190483         25         9         48           2         3         19         8         2187         19         12         45           3         7         19         9         8         2187         19         15         42           5         7         19         9         8192         19         15         42           5         2         19         5         8192         19         15         42           7         2         19         7         2048         19         21         36           3         2         19         27         2048         19         21         36           2         3         19         128         24         33         19         24         33           2         19         25         502         19         25         32         25         32           5         2         19         25         512         19         25         32         32           5         7         3         8         49         46561         12         4				25				32	57
3         2         19         3         32768         19         9         48         8         2187         19         12         45         5         7         19         9         9         49         19         15         42         42         19         15         42         19         15         42         19         15         42         19         15         42         19         15         42         19         15         42         19         15         42         19         15         42         19         15         42         19         15         42         19         21         36         32         19         128         2048         19         21         36         33         19         124         33         19         24         33         19         24         33         19         24         33         19         24         33         19         24         33         19         24         33         33         16         40         42         33         11         19         225         32         22         32         32         19         25         32         22         32	5			25					57
3         7         19         9         49         19         15         42           3         2         19         9         8192         19         15         42           7         2         19         7         2048         19         21         36           3         2         19         7         2048         19         21         36           2         19         27         2048         19         21         36           2         19         27         2048         19         21         36           2         11         19         128         111         19         24         33           3         19         128         11         19         25         32           2         19         25         512         19         25         32           2         19         25         512         19         25         32           2         19         25         32         12         42         42           3         2         19         25         32         12         42         42         43	3	2		3					57
3         7         19         5         49         19         15         42           5         2         19         9         8192         19         15         42           7         2         19         7         2048         19         21         36           3         2         19         27         2048         19         21         36           2         3         19         128         243         19         24         33           2         11         19         24         33         32         211         19         26         33           5         2         19         25         1024         19         25         32           5         2         19         25         1024         19         25         32           5         2         19         25         32         1024         19         25         32           5         2         19         25         32         33         16         40         40         40         40         40         40         40         40         40         40         40 <td< td=""><td>2</td><td></td><td></td><td></td><td></td><td></td><td></td><td></td><td>57</td></td<>	2								57
3         2         19         9         8192         19         15         42           7         2         19         7         2048         19         21         36           3         2         19         27         2048         19         21         36           2         19         128         11         19         24         33           3         19         22         33         19         24         33           5         2         19         25         512         19         25         32           5         2         19         25         512         19         25         32           2         5         7         32         26         53         343         16         40           2         5         3         2         665         5661         40         40           2         5         3         2         665         5661         40         40           2         7         3         8         49         6561         12         42           3         1         7         11         3	3								57 57
5         2         19         5         8192         19         15         42         18         21         36         33         2         19         77         2048         19         21         36         33         33         33         39         128         243         19         24         33         34         16         40         4	3								57
7	5								57
2	7								57
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5         2         19         25         1024         19         25         32         2         5         32         2         5         5         32         125         343         16         40         2         5         7         16         125         343         16         40         2         2         5         7         16         125         343         16         40         40         2         2         5         7         11         343         16         40         40         2         2         7         3         8         49         6561         12         42         2         17         11         6561         12         33         19         7         11         6561         12         33         2         27         33         49         17         9         42         2         2         17         9         42         2         17         9         42         2         17         9         42         2         2         17         9         42         2         2         17         9         42         2         2         17         12         39         9	2								57
5         2         19         25         512         19         25         32         125         343         16         40         22         5         7         16         125         343         16         40         22         5         7         16         125         343         16         40         40         22         5         343         16         40         40         22         5         343         16         40         40         22         25         81         6561         12         42         25         81         6561         17         99         42         21         33         37         7         17         3         49         17         19         42         22         21         33         17         8         17         99         42         22         21         31         17         8         729         17         12         39         22         27         25         2048         17         15         36         22         27         5         2048         17         15         36         22         27         5         2048         17         15         36         <	2			128					57 57
2	2			25					57
2	2			32					56
2 7 3 8 49 6561 12 12 37 11 3 5 13 3 5 13 6561 15 39 7 11 3 7 11 6561 15 39 17 11 6561 15 39 17 11 6561 15 39 17 17 9 42 17 9 42 17 9 42 17 9 42 18 18 18 18 18 18 18 18 18 18 18 18 18					125	343	16	40	56
5         13         3         5         13         6561         15         39           5         3         2         25         81         65536         25         27           3         7         17         3         49         17         9         42           2         13         17         8         13         17         12         39           2         13         17         8         729         17         12         39           2         13         17         8         729         17         12         39           2         13         17         8         729         17         12         39           3         2         17         9         2048         17         15         36           2         3         17         128         81         17         24         27           2         7         5         2048         17         15         36         42           3         13         32768         15         33         32768         15         33         33         42         33         32768 <t< td=""><td>2</td><td></td><td></td><td></td><td>625</td><td></td><td></td><td></td><td>54</td></t<>	2				625				54
7	2								54
5         3         2         25         81         65536         25         27         3         2         17         3         49         17         9         42         2         13         17         8         13         17         12         39         39         2         17         12         39	5								54 54
3         7         17         3         8192         17         9         42         12         13         17         9         42         12         13         17         12         39         17         12         39         17         12         39         17         12         39         17         12         39         17         12         39         17         12         39         17         12         39         17         12         39         17         12         39         17         12         39         17         12         39         17         12         39         11         15         36         2         17         15         36         17         15         36         2         17         15         36         2         17         15         36         2         17         15         36         2         17         15         36         2         17         15         36         2         17         15         36         2         17         15         36         2         17         30         31         31         32         32         33         33         32									52
3         2         17         3         8192         17         9         42         39           2         13         17         8         729         17         12         39           3         2         17         9         2048         17         15         36           5         2         17         5         2048         17         15         36           2         3         17         128         81         17         15         36           2         7         5         4         49         625         8         42         27           3         13         2         3         13         32768         9         39				3					51
The color of the	3				8192		9		51
3         2         17         9         2048         17         15         36         2           5         2         17         5         2048         17         15         36         2           2         3         17         128         81         17         24         27           2         7         5         4         49         625         8         42           3         13         2         3         13         32768         9         39           5         3         2         5         243         32768         15         33           3         11         2         9         111         32768         15         33           3         11         2         9         111         32768         15         33           3         11         2         5         113         32768         21         27           7         5         2         2         7         25         16384         21         25           3         5         2         27         25         16384         21         25           4 </td <td>2</td> <td></td> <td></td> <td></td> <td></td> <td></td> <td></td> <td></td> <td>51</td>	2								51
5         2         17         15         2048         17         15         36         2         27         5         4         49         625         8         42         27         5         4         49         625         8         42         27         3         3         13         32768         9         39	5								51 51
2	3								51
2         7         5         4         49         625         8         42         3           3         13         32768         15         33         42         3         32768         15         33         43         32768         15         33         43         33         43         43         43         43         42         42         42         43         43         43         43         43         43         43         43         43         43         43         44         49         45         42         42         43         43         44         49         43         44         49         43         44         49         43         44         49         43         44         49         44									51
3         13         2         3         13         32768         15         33         33         4           3         11         2         9         111         32768         15         33         4           5         11         2         9         111         32768         15         33         4           7         3         2         7         81         32768         21         27         25         16384         21         25         4         25         128         21         25         4         25         25         16384         21         25         4         25         2187         20         25         4         22         25         2187         20         25         4         22         25         2187         20         25         4         22         2187         20         25         4         4         21         23         3         11         21         24         4         4         21         23         3         11         49         9         33         4         4         2         11         3         4         4         2         2187									50
3         11         2         9         11         32768         15         33         4           5         11         2         5         11         32768         15         33         4           7         3         2         7         81         32768         21         27         25         16384         21         25         4           3         5         2         27         25         16384         21         25         4           2         11         3         8         11         2187         12         25         4           2         11         3         8         11         2187         20         25         4           3         11         7         3         11         49         9         33         4           3         11         7         3         11         49         9         33         4           3         11         2         3         11         8192         9         33         4           3         11         2         3         11         8192         9         33         4 </td <td>3</td> <td></td> <td></td> <td></td> <td></td> <td></td> <td></td> <td></td> <td>48</td>	3								48
5         11         2         5         11         32768         15         33         4           7         3         2         7         81         32768         21         27         4           7         5         2         7         25         16384         21         25         4           3         5         2         27         25         16384         21         25         4           2         11         3         8         11         2187         20         25         4           2         5         3         64         25         2187         20         25         4           3         11         7         3         11         49         9         33         4           3         11         7         3         11         8192         21         24         4           3         11         2         3         11         8192         29         33         4           5         3         7         2         27         7         8192         21         21         21         24         25         22									48
7         3         2         7         81         32768         21         27         4           7         5         2         7         25         16384         21         25         4           3         5         2         27         25         16384         21         25         4           2         11         3         8         11         2187         12         33         4           2         5         3         64         25         2187         20         25         4           3         11         7         3         11         49         9         33         4           3         11         7         3         11         49         9         33         4           5         3         7         5         81         49         15         27         4         4           3         11         2         3         11         8192         9         33         4         4         9         33         4         4         9         15         27         4         4         4         4         9         15									48 48
7         5         2         7         25         16384         21         25         4           3         5         2         27         25         16384         21         25         4           2         11         3         8         11         2187         12         23         33         2         25         4         4         25         2187         20         25         4         4         4         4         25         2187         20         25         4									48
3         5         2         27         25         16384         21         25         4           2         11         3         8         11         2187         20         25         4           2         5         3         64         25         2187         20         25         4           3         11         7         3         11         49         9         33         4           3         11         7         3         11         49         9         33         4           5         3         7         5         81         49         15         27         33         11         8192         9         33         4         49         15         27         4         49         15         27         4         49         15         27         33         11         8192         9         33         4         49         15         27         27         3         27         27         8         8192         15         27         21         27         3         3         2         21         21         21         22         21         21									46
2     11     3     8     11     2187     12     33     4       2     5     3     64     25     2187     20     25     4       3     11     7     3     11     49     9     33     4       3     11     7     3     11     49     9     33     4       5     3     7     5     81     49     15     27     4       3     11     2     3     11     8192     9     33     4       5     3     2     5     81     8192     9     33     4       5     3     2     5     81     8192     9     33     4       3     7     2     27     7     8192     21     21     21     22       3     7     2     27     7     8192     21     21     21     22     21     21     21     22     27     3									46
7         2         3         7         128         2187         21         24         48           3         11         7         3         11         49         9         33         48           5         3         7         5         81         49         15         27         48           3         11         8192         9         33         49         15         27         48           5         3         2         5         81         8192         15         27         48           3         7         2         27         7         8192         21         21         21         22         27         33         15         27         48         38         31         31         31         31         31         31         31         32         33         31         32         33         3	2				11				45
3         11         7         3         11         49         9         33         49         15         27         49           3         11         2         3         11         8192         9         33         49           5         3         2         5         81         8192         9         33         49           3         7         2         27         7         8192         21         21         21         21         23         21         21         22         22         23         22         23         23         23         24         24         24         24         25         24         24         25         24         33         15         24         25         24         33         15         24         25         24         33         33         34         <					25				45
5     3     7     5     81     49     15     27     4       3     11     2     3     11     8192     9     33     4       5     3     2     5     81     8192     15     27     4       3     7     2     27     7     8192     21     21     21       3     5     2     9     25     4096     15     25     4       3     7     2     9     25     4096     15     25     4       5     2     13     8     81     13     12     27     3       3     2     13     9     128     13     15     24     3       5     2     13     5     128     13     15     24     3       5     2     3     5     128     729     15     24     3       5     7     2     9     7     2048     15     21     3       5     7     2     2     5     27     2048     15     21     3       2     5     3     4     25     243     8     25     3									45 42
5         3         2         5         81         8192         15         27         4           3         7         2         27         7         8192         21         21         21         21         23           3         5         2         9         25         4096         15         25         21         21         24         27         33         3         12         27         33         3         12         27         33         3         12         27         33         3         15         24         33         15         24         33         3         15         24         33         3         15         24         33         3         15         24         33         3         15         24         33         3         15         24         33         3         15         24         33         3         15         24         33         3         15         24         33         3         24         33         3         20         33         3         21         33         33         33         33         33         33         33         33         33									
5         3         2         5         81         8192         15         27         4           3         7         2         27         7         8192         21         21         21         21         23           3         5         2         9         25         4096         15         25         21         21         24         27         33         3         12         27         33         3         12         27         33         3         12         27         33         3         15         24         33         15         24         33         3         15         24         33         3         15         24         33         3         15         24         33         3         15         24         33         3         15         24         33         3         15         24         33         3         15         24         33         3         15         24         33         3         24         33         3         20         33         3         21         33         33         33         33         33         33         33         33         33	3		2	3	11	8192	9	33	42 42
3         7         2         27         7         8192         21         21         23         21         23         24         25         4096         15         25         4096         15         25         4096         15         25         4096         15         25         4096         15         22         33         3         128         13         15         24         33         15         24         33         3         15         24         33         3         15         24         33         3         15         24         33         3         15         24         33         3         15         24         33         3         3         15         24         33         3         24         33         3         20         3         3         20         3         3         20         3         3         20         3         3         20         3	5	3	2	5	81	8192	15	27	42
3     5     2     9     25     4096     15     25     4       3     13     13     13     12     27     2       5     2     13     5     128     13     15     24       5     2     3     5     128     729     15     24       3     7     2     9     7     2048     15     21       5     7     2     5     7     2048     15     21       5     3     2     5     27     2048     15     21       2     5     3     4     25     243     8     25       2     7     3     8     7     243     12     21       2     5     11     8     25     3       3     2     11     3     128     11     9     24       2     7     11     8     7     11     12     21       2     3     11     8     27     11     12     21       2     3     11     8     27     11     12     21       2     3     5     2     7     25     4			2	27	7	8192	21	21	42
3     13     13     15     12     27       3     2     13     9     128     13     15     24       5     2     13     5     128     729     15     24       3     7     2     9     7     2048     15     21       5     7     2     5     7     2048     15     21       5     3     2     5     27     2048     15     21       2     5     3     4     25     243     8     25       2     7     3     8     7     243     12     21       2     5     11     4     25     11     8     25       3     2     11     3     128     11     9     24       2     7     11     8     7     11     12     21       2     3     11     8     27     11     12     21       2     3     11     8     27     11     12     21       2     3     5     2     7     25     4     21       2     3     5     2     7     25     4		5	2	9	25		15	25	40
5     2     13     5     128     13     15     24       5     2     3     5     128     729     15     24       3     7     2     9     7     2048     15     21       5     7     2     5     7     2048     15     21       5     3     2     5     27     2048     15     21       2     5     3     4     25     243     8     25       2     7     3     8     7     243     12     21       2     5     11     4     25     11     8     25       3     2     11     3     128     11     9     24       2     7     11     8     7     11     12     21       2     7     11     8     7     11     12     21       2     3     11     8     7     11     12     21       2     3     11     8     27     11     12     21       2     3     5     2     7     25     4     21       2     3     5     2     7		3	13	5	129	13	12	24	39
5     2     3     5     128     729     15     24       3     7     2     9     7     2048     15     21       5     7     2     5     7     2048     15     21       5     3     2     5     27     2048     15     21       2     5     3     2     5     243     8     25       2     7     3     8     7     243     12     21       2     5     11     4     25     11     8     25       3     2     11     3     128     11     9     24       2     7     11     8     7     11     12     21       2     7     11     8     27     11     12     21       2     3     11     8     27     11     12     21       2     3     11     8     27     11     12     21       2     3     8     5     81     12     15       3     2     5     3     32     25     4     21       2     3     3     32     25     9 <td< td=""><td></td><td>2</td><td>13</td><td></td><td>128</td><td>13</td><td>15</td><td>24</td><td>39</td></td<>		2	13		128	13	15	24	39
3         7         2         9         7         2048         15         21         3           5         7         2         5         7         2048         15         21         3           5         3         2         5         27         2048         15         21         3           2         5         3         4         25         243         8         25         3           2         7         3         8         7         243         12         21         3           2         7         11         8         25         11         8         25         3           3         2         11         3         128         11         9         24         3           2         7         11         8         27         11         12         21         3           2         7         11         8         27         11         12         21         3           2         7         5         2         7         25         4         21         3           3         2         5         3         32	5	2	3	5	128	729	15	24	39
5         7         2         5         7         2048         15         21         3           5         3         2         5         27         2048         15         21         3           2         5         3         4         25         243         8         25           2         7         3         8         7         243         12         21         3           2         5         11         4         25         11         8         25         3           3         2         11         3         128         11         9         24         3           2         7         11         8         27         11         12         21         3           2         3         11         8         27         11         12         21         3           2         5         3         8         27         25         4         21         3           2         5         3         5         2         27         25         4         21         2           3         2         5         3         32<	3	7	2	9	7	2048	15	21	36
5         3         2         5         27         2048         15         21         3           2         5         3         4         25         243         8         25         3           2         7         3         8         7         243         12         21         3           2         5         11         4         25         11         8         25         3           3         2         11         3         128         11         9         24         3           2         7         11         8         27         11         12         21         3           2         3         11         8         27         11         12         21         3           2         5         3         8         5         81         12         15         2           2         7         25         4         21         2         2         2         7         25         4         21         2           3         2         5         3         32         25         9         16         3           3 <td>5</td> <td></td> <td>2</td> <td>5</td> <td>7</td> <td>2048</td> <td>15</td> <td>21</td> <td>36</td>	5		2	5	7	2048	15	21	36
2     7     3     8     7     243     12     21       2     5     11     4     25     11     8     25       3     2     11     3     128     11     9     24       2     7     11     8     27     11     12     21       2     3     11     8     27     11     12     21       2     5     3     8     5     81     12     15       2     3     5     2     27     25     4     21       2     3     5     2     27     25     4     21       3     2     5     3     32     25     9     16       3     2     5     3     16     25     9     16       3     5     2     3     5     128     9     15       3     2     7     3     8     7     9     12	5		2	5	27	2048	15	21	36
2         5         11         4         25         11         8         25         3           3         2         11         3         128         11         9         24         3           2         7         11         8         7         11         12         21         3           2         3         11         8         27         11         12         21         3           2         5         3         8         5         81         12         15         2           2         7         25         4         21         3         2         25         4         21         3           3         2         5         3         32         25         9         16         3           3         5         2         3         5         128         9         15         3           3         2         7         3         8         7         9         12         3	5	7	2		2	243		21	33 77
3         2         11         3         128         11         9         24         3           2         7         11         8         7         11         12         21         3           2         3         11         8         27         11         12         21         3           2         5         3         8         5         81         12         15         2           2         3         5         2         27         25         4         21         2           3         2         5         3         32         25         9         16         3           3         2         5         3         16         25         9         16         3           3         5         2         3         5         128         9         15         3           3         2         7         3         8         7         9         12         3	2	ś	11	4	25	11		25	33
2     7     11     8     7     11     12     21     3       2     3     11     8     27     11     12     21     3       2     5     3     8     5     81     12     15     2       2     3     5     2     27     25     4     21     2       2     3     5     2     27     25     4     21     2       3     2     5     3     32     25     9     16     2       3     5     2     3     5     128     9     15     2       3     2     7     3     8     7     9     12     2	3	2	11	3	128	11	9	24	33
2     3     11     8     27     11     12     21     3       2     5     3     8     5     81     12     15     2       3     7     5     2     7     25     4     21     2       2     3     5     2     27     25     4     21     2       3     2     5     3     32     25     9     16     2       3     2     5     3     16     25     9     16     2       3     5     2     3     5     128     9     15     2       3     2     7     3     8     7     9     12     2	2	7	11	8	7	11	12	21	33
2	2	3	11	8	27	11	12	21	33
1     7     5     2     7     25     4     21     2       2     3     5     2     27     25     4     21     2       3     2     5     3     32     25     9     16     2       3     5     2     3     16     25     9     16     2       3     5     2     3     5     128     9     15     2       3     2     7     3     8     7     9     12     2		5	3	8	5	81		15	27
3     2     5     3     32     25     9     16     3       3     2     5     3     16     25     9     16     3       3     5     2     3     5     128     9     15     3       3     2     7     3     8     7     9     12     3			2	2	7	20 %		21	/ 20 %
3     2     5     3     16     25     9     16       3     5     2     3     5     128     9     15       3     2     7     3     8     7     9     12			5	3	32	25			25
3     5     2     3     5     128     9     15     2       3     2     7     3     8     7     9     12     2	3	2	5	3	16	25		16	25
3 2 7 3 8 7 9 12 2	3	5	2	3	5	128	9	15	24
	3	2		3	8	7	9	12	21

P1	P2	Р3	x	У	Z	S(x^n)	S(y <sup>n</sup> )	\$(z^n)
7	11	5	7	121	78125	35	110	145
2	17	5	2048 4096	17 6561	78125 78125	60 64	85 81	145 145
13	3 2	5 5	13	32768	78125	65	80	145
5	11	3	5	121	1594323	25	110	135
11	2	3	11	32768	1594323	55	80	135
7	2	3	49	16384	1594323	63	72	135
2	3	13 13	8 5	177147 59049	1 <del>69</del> 169	16 25	114 105	130 130
5 2	7	13	64	343	169	32	98	130
7	19	13	7	19	169	35	95	130
3	5	13	81	625	169	45	85	130
5	17	13	25	17	169	45	85	134
3	17	13	81	17 2187	169 169	45 55	85 75	130
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2	7	3	32	343	531441	28	98	12
2	3	7	4	177147	2401	12	114	12
2	11	7	8	121	2401	16	110	12
8	3	7	25	6561	2401	45 54	81 72	12 12
3	2	7	243 64	16384 19683	2401 156 <b>2</b> 5	32	93	12
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3	2	Ś	81	32768	15625	45	80	12
2	13	5	2048	13	15625	60	65	12
7	2	23	7	32768	23	35	80	11
11	2	23	11	2048	23 177147	55 16	60 98	11 11
2	7	3 11	8	343 343	121	12	98	11
2	7	11	3	343	121	12	98	11
5	17	11	5	17	121	25	85	11
7	3	11	7	2187	121	35	75	11
3	5	11	81	125	121	45	65	11
5	13	11	25	13 13	121 121	45 45	65 65	11
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5	2	3	25	2048	59049	45	60	10
2	3	5	4	19683	3125	12	93	10
2	3	5	16	6561	3125	24	81	10
3	2	5	27	16384	3125	33	72	10
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2	3	7	256	243	343	44	54	9
2	3	19	64	729	19	32	63	9
2	7	19	64	49	19	32	63	9
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2	5	3	2 2	625 17	19683 19683	8	85	9
2 5	17 2	3	5	8192	19683	25	68	9
2	5	3	32	125	19683	28	65	9
2	13	3	32	13	19683	28	65	9
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2	13	3	8	13	6561	16	65	1 8
5	11	2	5	11	32768	25	55	8
7	5	2	7	25	32768	35	45	5
7	3	2	7	81 49	32768 2187	35 12	45 63	5
2	7	2	4 27	7	8192	33	35	6
2	3	5	64	27	125	32	33	8
2	3	13	64	27	13 729	32	33	6
2	11	3	2	11	729	8	55	1
5	2	3	5	128	729 729	25	38 35	6
2	7	3	32	7 11	169	28 8	55	1 2
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3         5         13         9         390625         2197         30         250         20         10 <td< td=""><td></td><td></td><td></td><td></td><td>15625</td><td></td><td></td><td></td><td></td></td<>					15625				
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11         23         17         11         23         289         77         161         238           3         17         11         27         2401         1331         45         175         220           3         5         11         27         158625         1331         45         175         220           3         5         11         27         158625         1331         45         175         220           3         5         11         243         3125         1331         45         145         220           3         19         11         729         343         1331         87         133         220           3         7         11         729         343         1331         87         133         220           2         5         31         1024         3125         131         72         145         217           2         5         31         1024         3125         311         72         145         217           2         5         31         1024         3125         231         313         22         23         31 </td <td></td> <td></td> <td></td> <td></td> <td></td> <td></td> <td></td> <td></td> <td></td>									
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3         5         11         27         15625         1331         45         175         220           3         5         11         243         3125         1331         75         145         220           3         7         11         729         343         1331         87         133         220           2         5         7         1024         3125         16807         72         145         221           2         5         31         1024         3125         16807         72         145         221           5         11         29         25         121         29         60         143         203           3         11         29         256         121         29         60         143         203           2         11         29         256         121         29         60         143         203           3         5         7         9         3125         2601         30         143         103           2         11         7         16         121         2401         32         143         175									
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2         7         11         128         49         121         52         91         143           2         13         11         128         13         121         52         91         143           2         3         19         4         6561         19         16         117         133           2         3         19         64         729         19         46         87         133           2         3         7         4         6561         343         16         117         133           2         3         7         64         729         343         46         87         133           5         2         3         25         1024         19683         60         72         132           2         3         5         256         81         625         60         60         120           2         3         17         16         729         17         32         87         119           5         2         3         7         4         243         49         16         75         91           3	2					121			
2         3         19         4         6561         19         16         117         133           2         3         19         64         729         19         46         87         133           2         3         7         4         6561         343         16         117         133           2         3         7         64         729         343         46         87         133           5         2         3         25         1024         19683         60         72         132           2         3         5         256         81         625         60         60         120           2         3         17         16         729         17         32         87         119           5         2         3         5         1024         2187         30         72         102           2         3         7         4         243         49         16         75         91           3         2         7         27         64         49         45         46         91           2         3	2	7	11	128	49	121	52	91	143
2         3         19         64         729         19         46         87         133           2         3         7         4         6561         343         16         117         133           2         3         7         64         729         343         46         87         133           5         2         3         25         1024         19683         60         72         132           2         3         5         256         81         625         60         60         120           2         3         17         16         729         17         32         87         119           5         2         3         5         1024         2187         30         72         102           2         3         7         4         243         49         16         75         91           3         2         7         27         64         49         45         46         91           2         3         13         4         243         13         16         75         91           3         2 <t< td=""><td>2</td><td></td><td></td><td>128</td><td>13</td><td>121</td><td></td><td></td><td>143</td></t<>	2			128	13	121			143
2     3     17     16     729     17     32     87     119       5     2     3     5     1024     2187     30     72     102       2     3     7     4     243     49     16     75     91       3     2     7     27     64     49     45     46     91       2     3     13     4     243     13     16     75     91       3     2     13     27     64     13     45     46     91       3     2     5     3     1024     125     18     72     90       3     2     5     9     256     125     30     60     90       2     7     3     32     7     729     38     49     87       2     3     11     16     27     11     32     45     77	2				729	19			133
2     3     17     16     729     17     32     87     119       5     2     3     5     1024     2187     30     72     102       2     3     7     4     243     49     16     75     91       3     2     7     27     64     49     45     46     91       2     3     13     4     243     13     16     75     91       3     2     13     27     64     13     45     46     91       3     2     5     3     1024     125     18     72     90       3     2     5     9     256     125     30     60     90       2     7     3     32     7     729     38     49     87       2     3     11     16     27     11     32     45     77	2	3	7	4	6561	343	16	117	133
2     3     17     16     729     17     32     87     119       5     2     3     5     1024     2187     30     72     102       2     3     7     4     243     49     16     75     91       3     2     7     27     64     49     45     46     91       2     3     13     4     243     13     16     75     91       3     2     13     27     64     13     45     46     91       3     2     5     3     1024     125     18     72     90       3     2     5     9     256     125     30     60     90       2     7     3     32     7     729     38     49     87       2     3     11     16     27     11     32     45     77	2	3		64 25	729 1024	343 10482			133
2     3     17     16     729     17     32     87     119       5     2     3     5     1024     2187     30     72     102       2     3     7     4     243     49     16     75     91       3     2     7     27     64     49     45     46     91       2     3     13     4     243     13     16     75     91       3     2     13     27     64     13     45     46     91       3     2     5     3     1024     125     18     72     90       3     2     5     9     256     125     30     60     90       2     7     3     32     7     729     38     49     87       2     3     11     16     27     11     32     45     77	2	3	5	256	81	625			120
2     3     7     4     243     49     16     75     91       3     2     7     27     64     49     45     46     91       2     3     13     4     243     13     16     75     91       3     2     13     27     64     13     45     46     91       3     2     5     3     1024     125     18     72     90       3     2     5     9     256     125     30     60     90       2     7     3     32     7     729     38     49     87       2     3     11     16     27     11     32     45     77	2	3	17	16	729	17	32	87	119
2 7 3 32 7 729 38 49 87 2 3 11 16 27 11 32 45 77	2	3		5	1024 243	2187 40	30 16	72	102 91
2 7 3 32 7 729 38 49 87 2 3 11 16 27 11 32 45 77	3	2	7	27	64	49		46	91
2 7 3 32 7 729 38 49 87 2 3 11 16 27 11 32 45 77	2	3		4	243	13		75	91
2 7 3 32 7 729 38 49 87 2 3 11 16 27 11 32 45 77	3	2	1.5	3	1024	15 125			91 90
2 7 3 32 7 729 38 49 87 2 3 11 16 27 11 32 45 77	3	2	5	9	256	125	30	60	90
5 7 2 5 0 264 30 30 40	2	7		32	7	729			87
	5	3	2	5	9	256	30	30	60

P1	PZ	Р3	х	У	ž	S(x°n)	S(y^n)	S(z°n)
17	53	41	17	2809	68921	187	1166	1353
29	47	41	29 37	2209	68921	319	1034	1353
37 11	43	41	1771561	1849 961	68921 68921	407 671	946 682	1353 1353
61	31	41	61	961	68921	671	682	1353
5	29	61	25	707281	3721	95	1247	1342
11	37	61	11	50653	3721	121	1221	1342
17	19	61	4913	130321	3721	544	798	1342
11	71 23	61 31	161051 243	71 6436343	3721	561 114	781 1219	1342 1333
47	71	59	47	71	923521 3481	517	781	1298
11	67	59	161051	67	3481	561	737	1298
5	19	29	5	47045881	707281	50	1197	1247
13	17	29	28561	83521	707281	533	714	1247
2	19	37	4	47045881	50653	24	1197	1221
17	47	37 37	17	2209	50653	187	1034	1221
29 53	41 29	37	29 53	1681 841	50653 50653	319 583	902 638	1221 1221
13	43	23	169	1849	6436343	273	946	1219
7	43	23	2401	1849	6436343	273	946	1219
5	17	53	25	24137569	2809	95	1071	1166
47	59	53	47	59	2809	517	649	1166
13	29	17	13	24389	24137569	143	928	1071
13	19	17 17	169 2401	130321	24137569 24137540	273	798	1071
7	19 19	47	2401 3	130321 2476099	24137569 2209	273 27	798 1007	1071 1034
11	73	47	121	73	2209	231	803	1034
23	71	47	23	71	2209	253	781	1034
11	53	47	14641	53	2209	451	583	1034
41	53	47	41	53	2209	451	583	1034
43	11	47	43	161051	2209	473	561	1034
5 3	67	19 31	15625 81	67 1681	2476099 29791	270 90	737 902	1007 992
7	41 59	31	16807	59	29791	343	649	992
7	13	43	49	4826809	1849	140	806	946
13	73	43	13	73	1849	143	803	946
19	67	43	19	67	1849	209	737	946
5	13	43	15625	371293	1849	270	676	946
3	37 71	29 41	243 11	1369 71	24389 1681	114	814	928 902
11 11	61	41	121	61	1681	121 231	781 671	902
23	59	41	23	59	1681	253	649	902
29	53	41	29	53	1681	319	583	902
31	11	41	31	161051	1681	341	561	902
7	37	17	7	1369	1419857	70	814	884
13 13	11 61	37 37	13 13	1771561 61	1369 1369	143 143	671 671	814 814
11	53	37	121	53	1369	231	583	814
23	11	37	23	161051	1369	253	561	814
5	17	37	15625	4913	1369	270	544	814
31	43	37	31	43	1369	341	473	814
11	43	37	1331	43	1369	341	473	814
7	23	13	7	12167 1771561	4826809 4826809	70	736	806
3 5	11	13 13	729 125	1771561	4826809	135 135	671 671	806 806
3	61	13	729	61	4826809	135	671	806
5	61	13	125	61	4826809	135	671	806
7	37	13	117649	37	4826809	399	407	806
19	37	13	361	37	4826809	399	407	806
11	31	73	11	961	73	121	682	803
13	13	73 71	15625 13	28561 841	73 71	270 143	533 638	803 781
11	29 23	67	121	529	67	231	506	737
2	13	23	32	371293	12167	60	676	736
7	13	23	343	28561	12167	203	533	736
19	43	31	19	43	961	209	473	682
11	41	31	121	41	961	231	451	682
3	59	13	3 64	59 6859	371293 371293	27	649	676
2 7	19 43	13 13	343	43	3/1293 371293	68 203	608 473	676 676
5	11	13	3125	14641	371293	225	451	676
5	41	13	3125	41	371293	225	451	676
29	17	13	29	289	371293	319	357	676
	23	59	13	529	59	143	506	649
13 11	47	29	11	47	841	121	517	638

#### 'SMAR iv, H. lbstedt, 930323

'This program searches for solutions to the equation  $S(k^n)^i = S(n^k)$ . The search is limited to the first 8000 values of S(n) loaded from the file SN.DAT. No non-trivial solutions were found

```
DEFLING I-S : DEFDBL X.Y.Z
CLS:WIDTH "LPT1:",120
DIM S(8000)
L=0:NS=90:KS=90
OPEN "SN.DAT" FOR INPUT AS #1
FOR I = 1 TO 8000
INPUT #1.S(L)
NEXT
CLOSE #1
PRINT S(8000)
LPRINT TAB(12) "Search for solutions to S(k^n)^i = S(n^k)."
LPRINT TAB(12) :LPRINT "-
LPRINT TAB(12) :LPRINT "
                                   | S(k^n)|
                                                         S(n^k)
                                                                      ŧ a
LPRINT TAB(12) :LPRINT "}
FOR K=2 TO KS : PRINT K
FOR N=2 TO NS
IF K^N>8000 OR N^K>8000 THEN N=NS:GOTO L2
C=S(K^N):D=S(N^K)
IF C>D THEN SWAP C,D
E = 1 : I = 0
L1:
E=E*C: |=|+1
IF E>D THEN L2
IF E=D AND K<>N THEN GOSUB LW
IF E < D THEN L1
L2:
NEXT
NEXT
LPRINT TAB(12) :LPRINT "L
LPRINT CHR$(12)
PRINT "END" :END
 LW:
LPRINT TAB(12) "] "; :LPRINT USING "######";K;
LPRINT " | "; :LPRINT USING "######";N;
LPRINT " | ": :LPRINT USING "######";S(K^N);
LPRINT " | "; :LPRINT USING "######";N;
LPRINT " | "; :LPRINT USING "######";K;
LPRINT " | "; :LPRINT USING "######";S(N^K);
LPRINT "|"; :LPRINT USING "#######;1;
LPRINT "I"
RETURN
```

Search for solutions to  $S(k^n)^i = S(n^k)$ .

k	n	S(k <sup>*</sup> n)	n	k	S(n^k)	i
2	4 2	6	4 2	2 4	6 6	1

#### 'SMAR v, H. lbstedt, 930323

Set l = 22 and NB = 62 on HPIIP

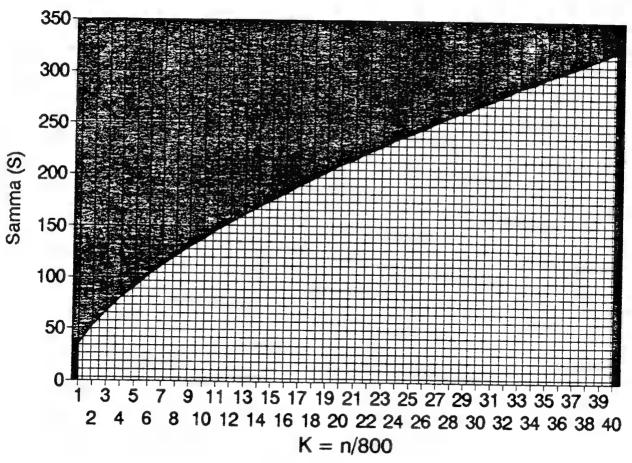
This program uses the first 32000 values of S(n) input from the file SN.DAT to calculate 1+1/S(2)+1/S(3)+...+1/S(n) for n=800, 1600, 2400, ... 32000. The sums are used to study the behaviour of 1+1/S(2)+1/S(3)+...+1/S(n)-T(n). The following cases are examined T(n)=0, T(n)=Log(S(n)), T(n) equal to the logarithm of the largest prime less than n and finally  $T(n)=(rK-V)+1/2^a+1/3^a+...+1/n^a$ , where a=.5164, r=0.96 and V=27. K=n/800.

```
'Number of intervals = NN (40), Size of interval NI (800),
DEFDBL A-Z:DIM LAM(40),SAM(40),ZAM(40),HAM(40)
NN = 40 : NI = 800
CLS: WIDTH "LPT1:".120
Z=1:K=1:Z1=0
LPRINT:LPRINT
LPRINT TAB(12); "Behaviour of 1+1/S(2)+1/S(3)+ ... 1/S(n)-T(n), K=n\800."
LPRINT TAB(12): "In the column LAM(K) T(n) = 0, in SAM(K) T(n) = Log(S(n)), in"
LPRINT TAB(12): "ZAM(K) T(n) is the logarithm of the largest prime less"
LPRINT TAB(12): "than \pi and in HAM(K) T(n) = 1+1/2^.52+1/3^.52+... 1/n^.52." :LPRINT
LPRINT TAB(12): "-
                                                                     Ţn
LPRINT TAB(12); "
                     ĸ
                              LAM(K)
                                         SAM(K)
                                                   ZAM(K)
                                                               HAM(K)
LPRINT TAB(12); "-
OPEN "SN DAT" FOR INPUT AS #1
WHILE K<41
G = 1
WHILE I < K*NI
INCR I
INPUT #1.S
IF S>G THEN G=S
Z=Z+1/S
Z1 = Z1 + 1/1^{5}.5164
WEND
LAM(K) = Z
HAM(K) = Z-Z1-.96*K+V
SAM(K) = Z-LOG(S)
ZAM(K) = Z-LOG(G)
LPRINT TAB(12); :LPRINT "1"; :LPRINT USING "#########";K;
LPRINT " | ": :LPRINT USING "#########":LAM(K):
LPRINT " | "; :LPRINT USING "#########";SAM(K);
LPRINT " | "; :LPRINT USING "#########";ZAM(K);
LPRINT "|"; :LPRINT USING "#########";HAM(K);
LPRINT "I"
INCR K
WEND
CLOSE #1
LPRINT TAB(12); "L
LPRINT :LPRINT TAB(12) "SMAR V"
LPRINT CHR$(12)
PRINT "END" :END
```

PCW, Numbers Count: Problem (v), February 1993

K	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20
s	35	53	67	80	91	102	112	121	130	138	146	154	162	169	178	183	190	197	203	210
Κ	21	22	23	24		1	27							34				38	39	40
s	216	223	228	235	240	246	252	258	262	268	273	279	285	289			_			

1+1/S(2)+...+1/S(n)-log(S(n))n = 800, 1600, 2400, ... 32000



Behaviour of  $1+1/S(2)+1/S(3)+\ldots 1/S(n)-T(n)$ .  $K=n\setminus 800$ . In the column LAM(K) T(n)=0, in SAM(K) T(n)=Log(S(n)), in ZAM(K) T(n) is the logarithm of the largest prime less than n and in HAM(K)  $T(n)=(r*K-V)+1/2^a+1/3^a+\ldots 1/n^a$ , where r=0.96, V=27 and a=0.5164 have been chosen to fit HAM(K) as closely as possible to 0.

K	LAM(K)	SAM(K)	ZAM(K)	HAM(K)
1	37	35	31	13
2	55	53	48	9
3	70	67	62	6
4	82	80	74	5
5	94	91	85	3
6	104	102	96	2
7	114	112	105	1
8	123	121	115	1
9	132	130	123	0
10	141	138	132	-0
11	149	146	140	-0
12	157	154	148	-1
13	164	162	155	-1
14	172	169	162	-1
15	179	176	170	-1
16	186	183	176	-1
17	193	190	183	-1
18	200	197	190	-1
19	206	203	196	-1
20	212	210	203	-1
21	219	216	209	-1
22	225	223	215	-1
23	231	228	221	-1
24	237	235	227	-1
25	243	240	233	-1
26	249	246	239	-1
27	254	252	244	-1
28	260	258	250	-1
29	265	262	255	-1
30	271	268	261	-1
31	276	273	266	-1
32	282	279	272	-1
33	287	285	277	-0
34	292	289	282	-0
35	297	295	287	-0
36	303	300	292	-0
37	307	304	297	-0
38	313	310	302	0
39	317	315	307	0
40	322	320	312	0

#### The Smarandache Function S(n)

Graphical representation of 1+1/S(2)+1/S(3)+...+1/S(n)-T(n) for n<32000.

Graph I:

T(n) = 0.

Graph II:

T(n) = log(S(n)).

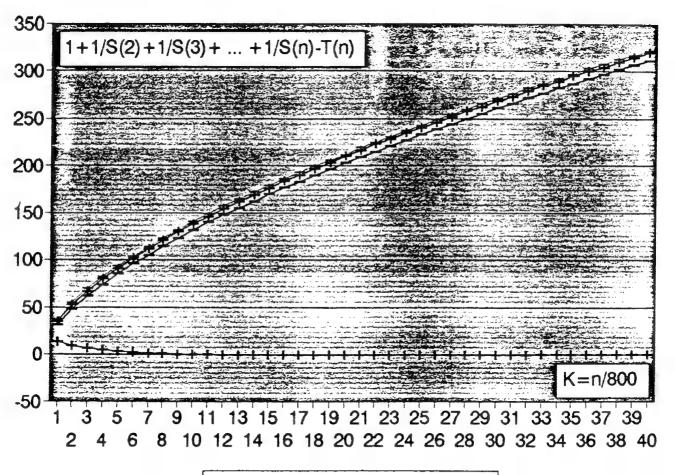
Graph III:

T(n) = log(largest prime < n).

Graph IV:

 $T(n) = (rK-V) + 1/2^a + 1/3^a + ... + 1/n^a$ , where the parameters r=0.96, V=27 and

a = 0.5164 were chosen to fit the graph as closely as possible to a horizontal line.



#### 'SMARAND1, H. Ibstedt, 930327

The Smarandache function S(n) calculated by comparing largest prime and  $S(P^A)$ . The upper limit for the calculation is n=1000000. The results are used to calculate  $1+1/S(2)+1/S(3)+\ldots+1/S(n)$  registering partial sums for n=25000, 50000, 75000, ... 1000000

```
DEFLNG A-S
CLS:T=TIMER
DIM P(168),D(168,20),K(168),L(168)
OPEN "PA" FOR INPUT AS #1
FOR I=1 TO 168:INPUT #1,P(I):NEXT:CLOSE #1
```

This part of the program calculates  $S(P(I)^A)$  and saves the result in the array D(I,A), P(I) is the Ith prime number. The routine uses the fact that  $D(I,A) < = P(I)^*A$  in the search for the value of D(I,A). This calculation goes as far as is required to calculate S(n) up to n = 1000000.

```
FOR I=1 TO 168
A=2:P=P(1):D(1,1)=P
WHILE A < 21
C=0:N=0
 L:
INCR C
INCR N.P.
IF C> = A THEN D(I.A) = N : GOTO LWEND
PP = P*P
L1:
IF N-PP*INT(N/PP) = 0 THEN INCR C :PP=PP*P :GOTO L1
IF C> = A THEN D(I,A) = N :GOTO LWEND :ELSE L
 LWEND:
INCR A
WEND
NEXT
```

This part of the program calculates S(N) and the sum of reciprocals. It calls on the subroutine NFACT to express N in prime factor form. Factors  $P(I)^A$  with A>1 are replaced by D(I,A) and placed in array L(I) together with the factors P(I) of multiplicity 1. S(N) is then the largest component of L(I). S(N) is stored in a file SN.DAT.

```
N=1:Z=1:D=0:ZC=0

OPEN "SAM.DAT" FOR APPEND AS #3

WHILE N < 1000001

if inkey$ < > "" then print "end" :end

INCR N :INCR D :PRINT N

'Factorize N.

GOSUB NFACT

IF K(0) > 0 THEN S = P(0) :GOTO LWR

'Construct L().

FOR I=1 TO 168:L(I) = 0 :NEXT

C=0

FOR I=1 TO M

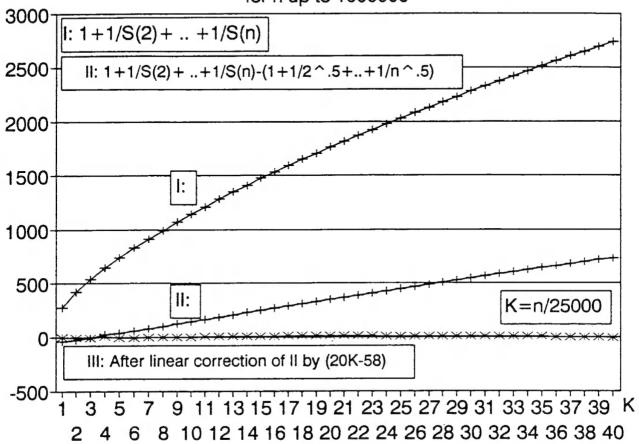
INCR C
```

```
IF K(I) = 1 THEN L(C) = P(I)
IF K(I) > 1 THEN L(C) = D(I, K(I))
NEXT
'Find the largest value of L() and hence S(N).
S = 0
FOR I=1 TO C
IF L(I) > S THEN S = L(I)
NEXT
 LWR:
Z=Z+1/S
IF D=25000 THEN ZC=ZC+Z:WRITE #3,Z,ZC:Z=0:D=0
WEND
CLOSE #3
T=TIMER-T:PRINTT
END
'Subroutine for factorization of N. (Improved from SMARAND to avoid large primes)
 NFACT:
FOR I = 0 TO 168 :K(I) = 0 :NEXT :P(0) = 0
N1 = N : I = 0 : M = 0
FOR I=1 TO 168
 LA:
|F|N1-P(I)*INT(N1/P(I)) = 0 THEN K(I) = K(I) + 1 : M = I : N1 = N1/P(I) : GOTO LA
IF N1 = 1 THEN I = 168
NEXT
IF N1 > 1 THEN P(0) = N1 : K(0) = 1
RETURN
```

Problem v: Summary of obtained data.

		Graph I		Graph II		Graph III
	Sum	Sum	Sum			after
K	interval	1/S(n)	1/n^2	Diff.	Lin. Corr.	lin. corr.
1	277	277	315	-38	-38	0
2	145	422	446	-24	-18	-6
3	119	541	546	-5	2	-7
4	105	646	621	25	22	3
5	96	742	706	36	42	-6
6	89	831	773	58	62	-4
7	83	914	835	79	82	-3
8	79	993	893	100	102	-2
9	76	1069	947	122	122	0
10	73	1142	999	143	142	1
11	70	1212	1047	165	162	3
12	68	1280	1094	186	182	4
13	66	1346	1139	207	202	5
14	64	1410	1182	228	222	6
15	63	1473	1223	250	242	8
16	61	1534	1263	271	262	9
17	60	1594	1302	292	282	10
18	58	1652	1340	312	302	10
19	57	1709	1377	332	322	10
20	56	1765	1413	352	342	10
21	55	1820	1448	372	362	10
22	54	1874	1482	392	382	10
23	53	1927	1515	412	402	10
24	52	1979	1548	431	422	9
25	52	2031	1580	451	442	9
26	51	2082	1611	471	462	9
27	50	2132	1642	490	482	8
28	50	2182	1672	510	502	8
29	49	2231	1701	530	522	8
30	49	2280	1731	549	542	7
31	48	2328	1759	569	562	7
32	47	2375	1787	588	582	6
33	47	2422	1815	607	602	5
34	46	2468	1842	626	622	4
35	46	2514	1869	645	642	3
36	45	2559	1896	663	662	1
37	45	2604	1922	682	682	0
38	44	2648	1948	700	702	-2
39	44	2692	1973	719	722	-3
40	44	2736	1999	737	742	-5

# The Smarandache Function S(n) Comparison with the sum of 1/n ^ 0.5 for n up to 1000000



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A collection of papers concerning Smarandache type functions, numbers, sequences, integer algorithms, paradoxes, experimental geometries, algebraic structures, neutrosophic probability, set, and logic, etc.

Dr. C. Dumitrescu & Dr. V. Seleacu Department of Mathematics University of Craiova, Romania;